

Aplicatii la cautarea neinformata si informata

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 - Parcurgerea in latime
 - Parcurgerea in adancime
 - Parcurgerea limitata in adancime
- Aplicatii la cautarea informata
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Formulara problemelor

- O problema se defineste prin patru puncte:
 1. **Starea initiala** in care se afla agentul (de exemplu, Arad).
 2. **Actiuni** sau **functia succesor** $S(x)$ – fiind data o stare x , $S(x)$ intoarce multimile de stari in care se poate ajunge din x printr-o singura actiune ($S(\text{Arad}) = \{\text{Zerind}, \text{Sibiu}, \text{Timisoara}\}$)
 3. **Testarea tintei problemei** – se verifica daca starea curenta a atins tinta problemei ($x = \text{Bucuresti}$, $\text{sah_mat}(x)$)
 4. Functia de **cost al drumului** –
 - calculeaza un cost g pentru drumul curent (suma distantelor, numarul actiunilor executate etc).
 - $c(x, y)$ – costul pasului, presupus sa fie ≥ 0
- O solutie este o secventa de actiuni care merg de la starea initiala la starea tinta

Algoritm general de cautare

functia *cautare_generala*(*problema*, *strategie*)

intoarce *solutie* sau *esec*

Initializeaza arborele de cautare folosind starea initiala a problemei.

Cat timp este posibil *executa*

Daca nu mai sunt posibilitati de incercat *atunci*

intoarce *esec*

Alege un nod posibil in concordanta cu strategia

Daca nodul contine o stare tinta *atunci*

intoarce *solutia* corespunzatoare

Altfel gaseste toate posibilitatile ce pornesc din acest nod si
adauga-le la arborele de cautare

Sfarsit cat timp

Algoritm general de cautare

functia cautare_generala(problema) **intoarce** solutie sau esec
noduri = genereaza_coada(genereaza_nod(stare_initiala[problema]))

Cat timp este posibil executa

Daca noduri = vida atunci

intoarce esec

nod = scoate_din_fata(noduri)

Daca testare_tinta[problema] se aplica la stare(nod) atunci

intoarce nod

Altfel

noduri = adauga(noduri, expandare(nod, actiuni[problema]))

Sfarsit cat timp

Algoritm cautare in latime

functia cautare_latime(problema) **intoarce** solutie sau esec

noduri = genereaza_coadă(genereaza_nod(stare_initiala[problema]))

Cat timp este posibil executa

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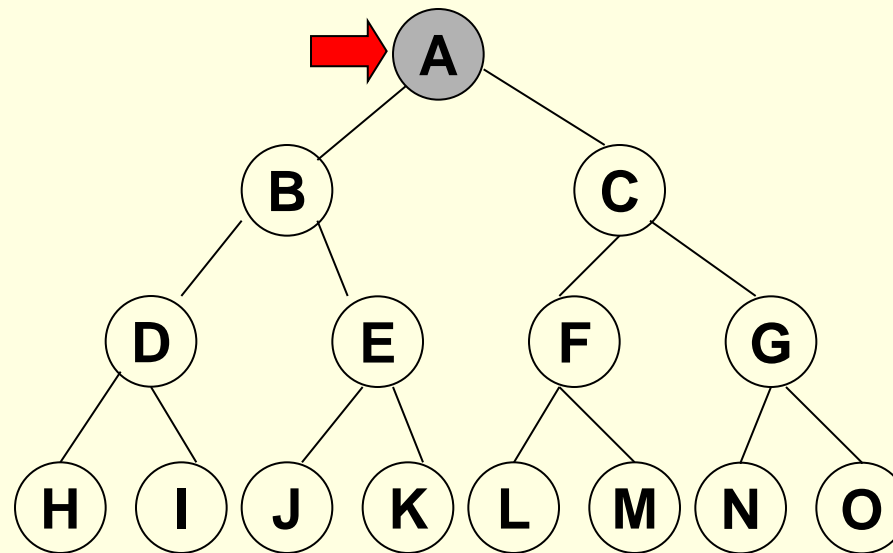
intoarce nod

Altfel

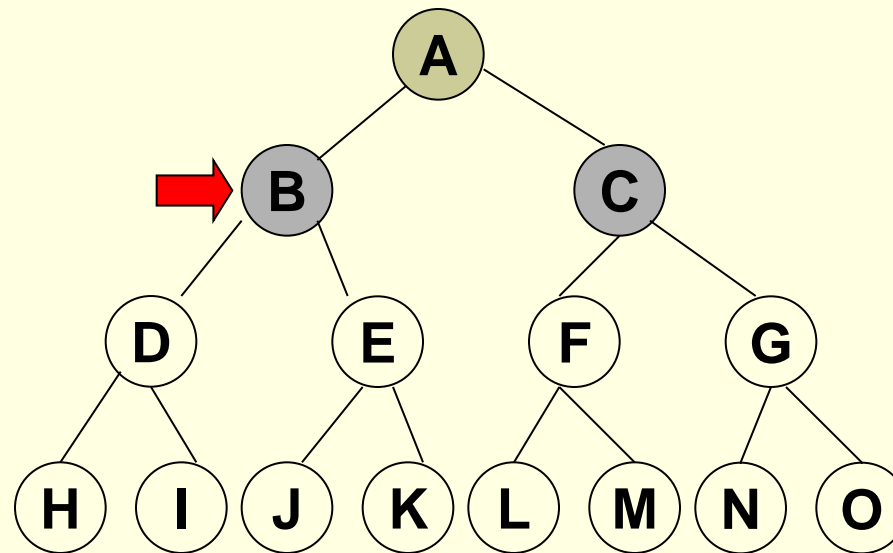
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Sfarsit cat timp

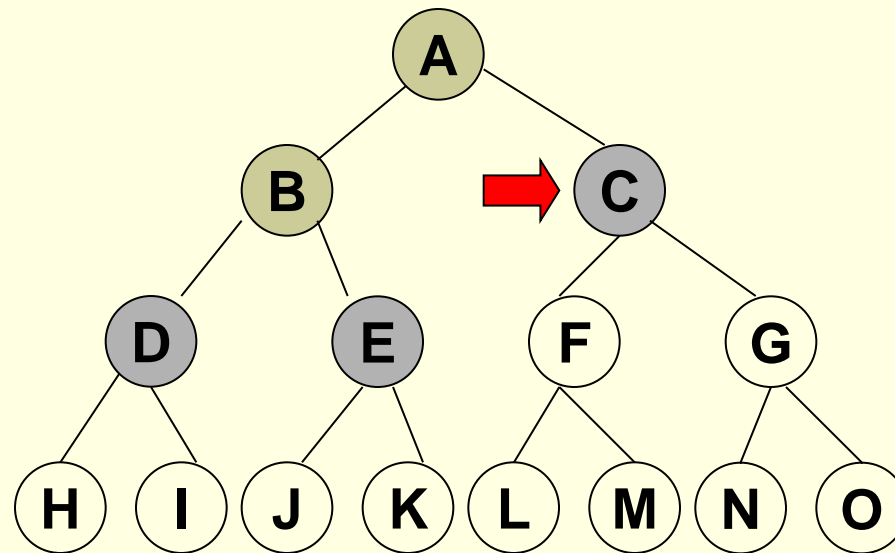
Cautarea in latime



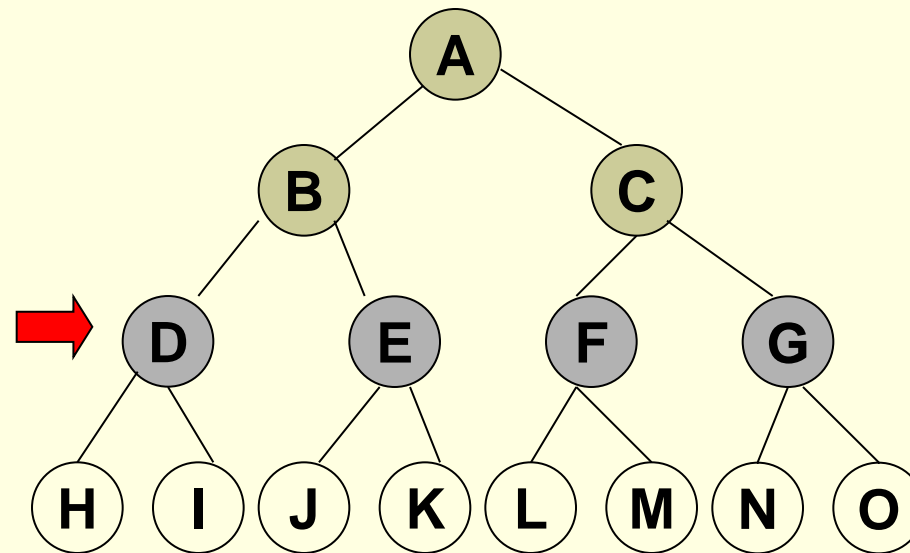
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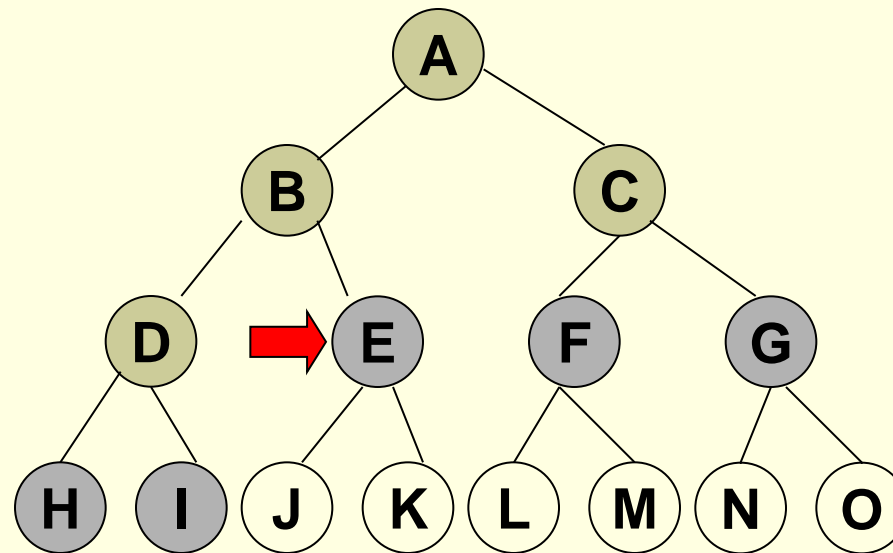
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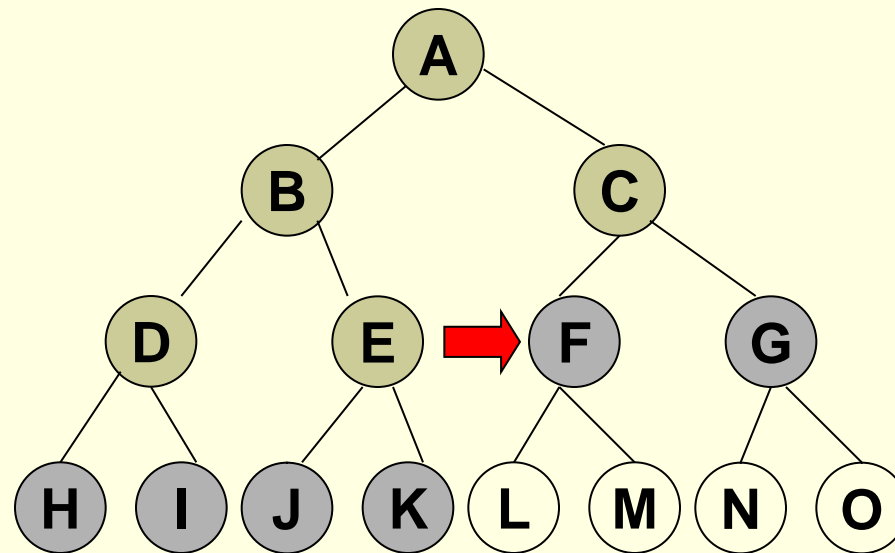
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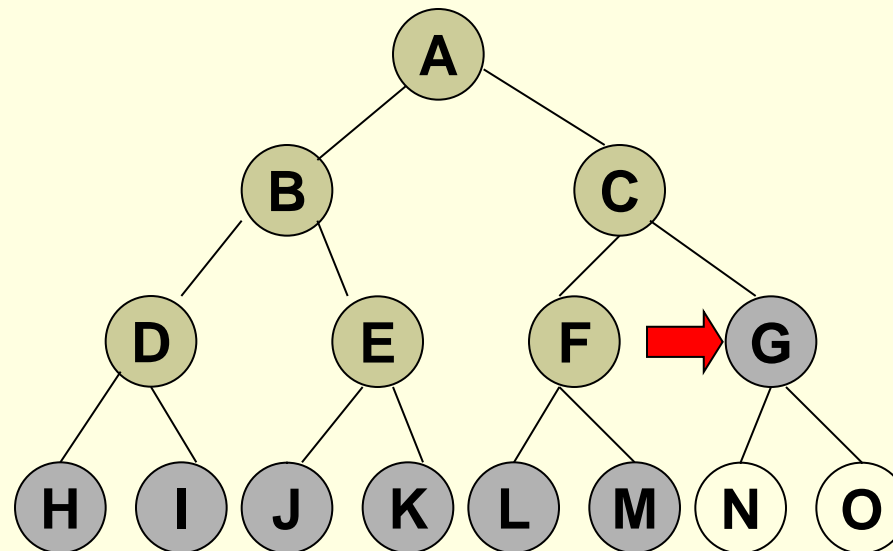
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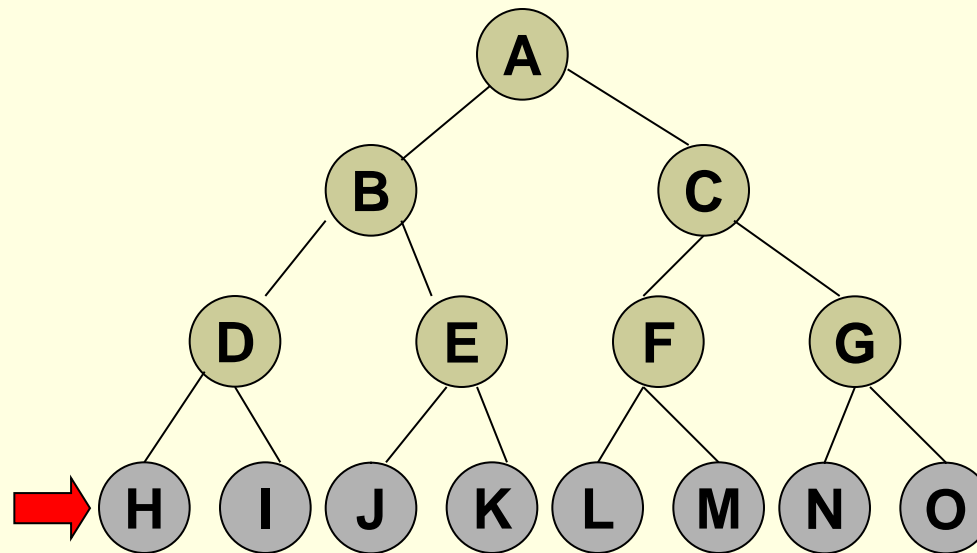
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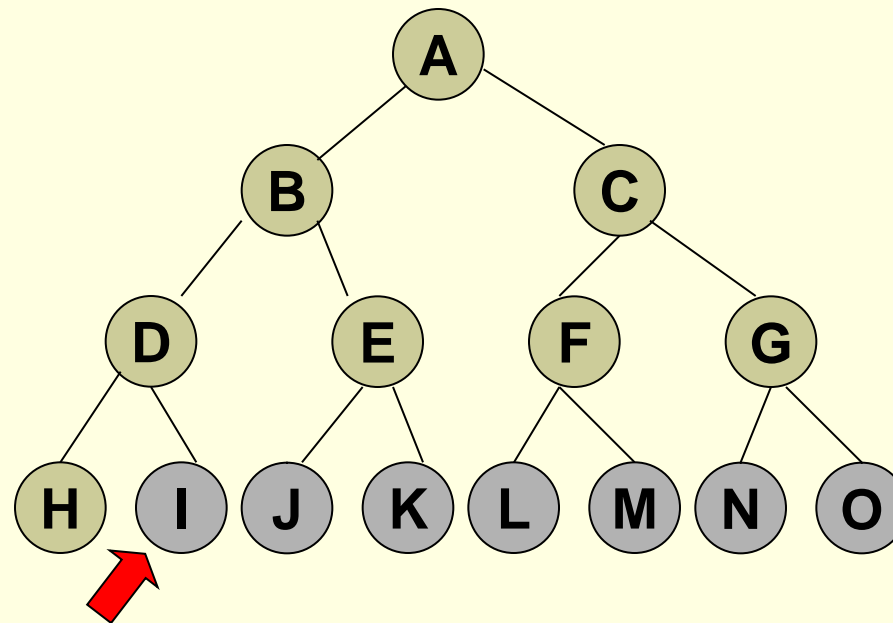
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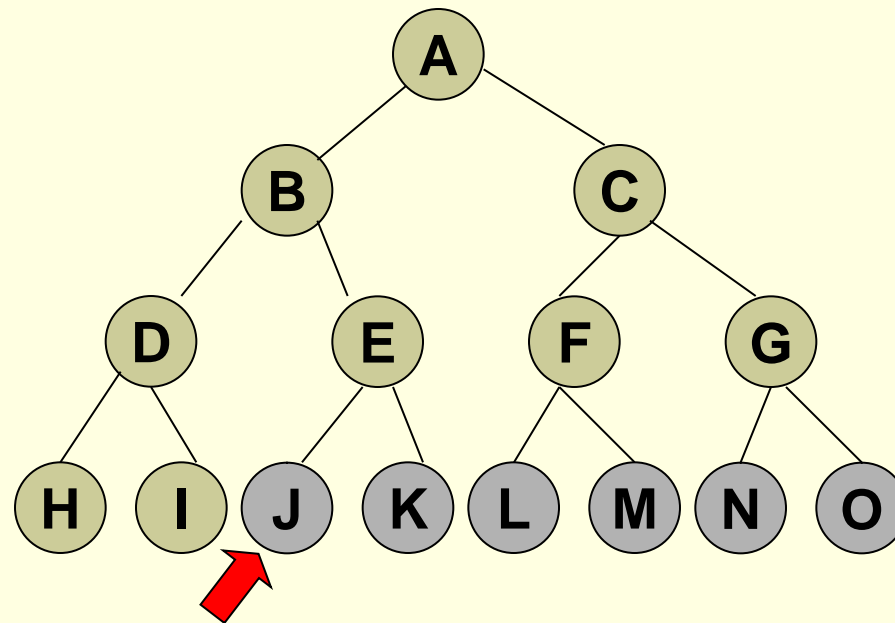
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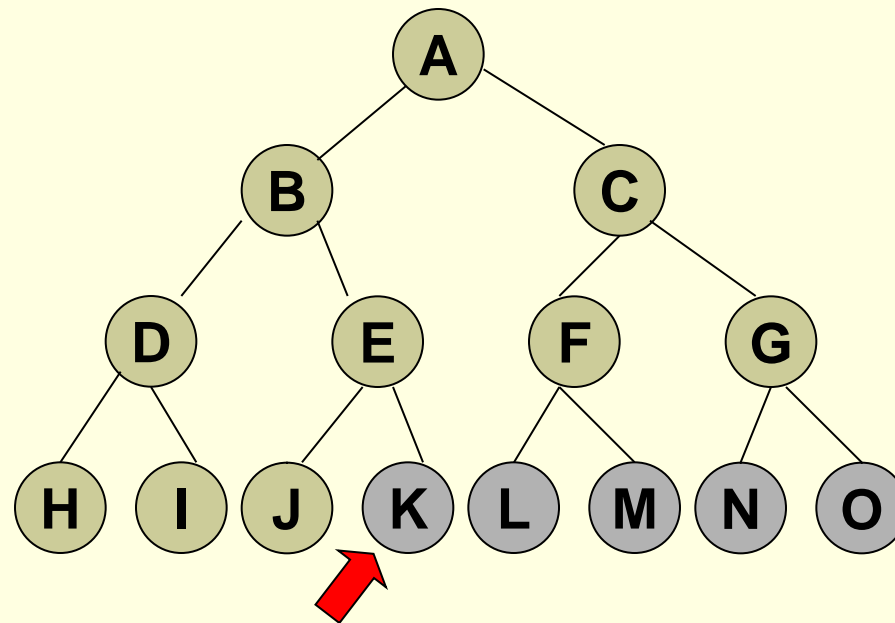
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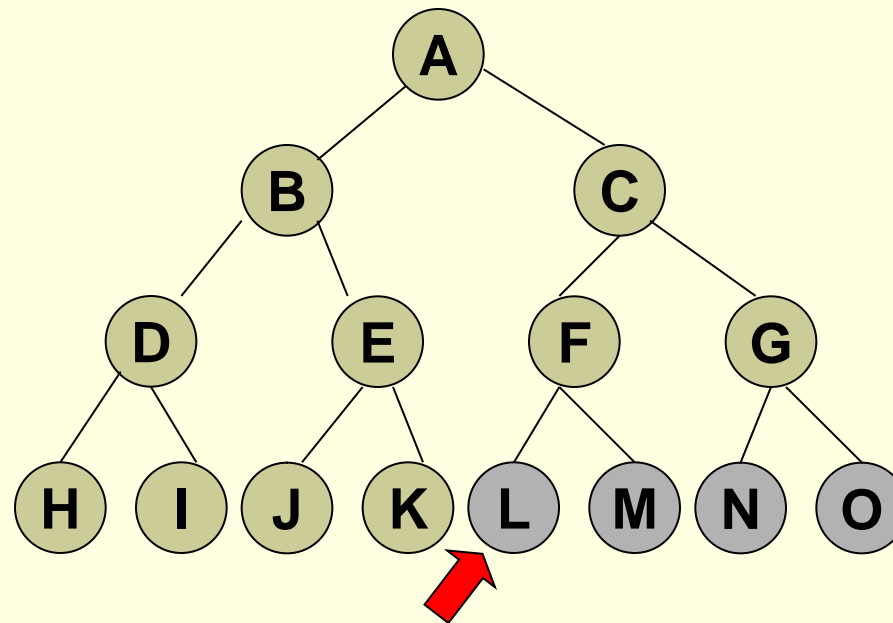
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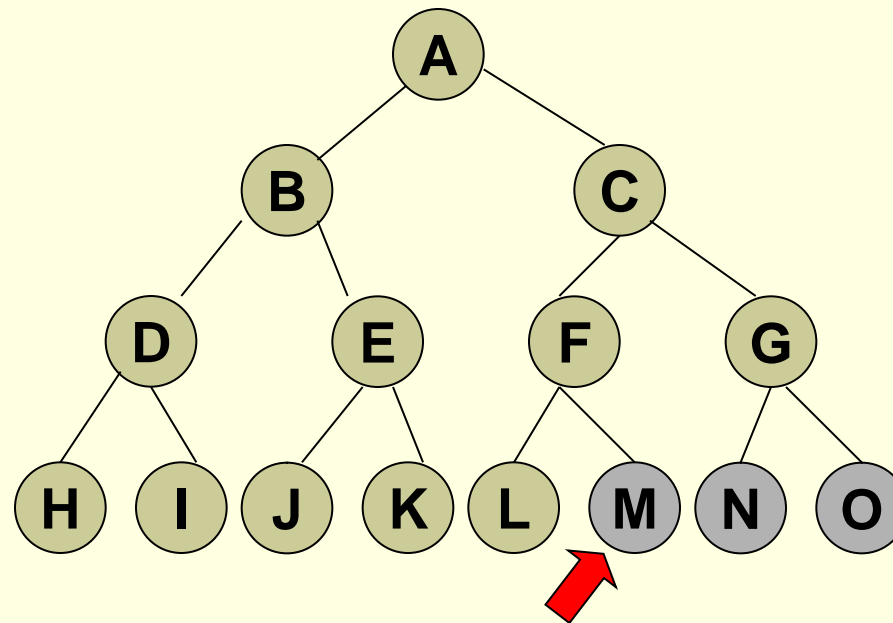
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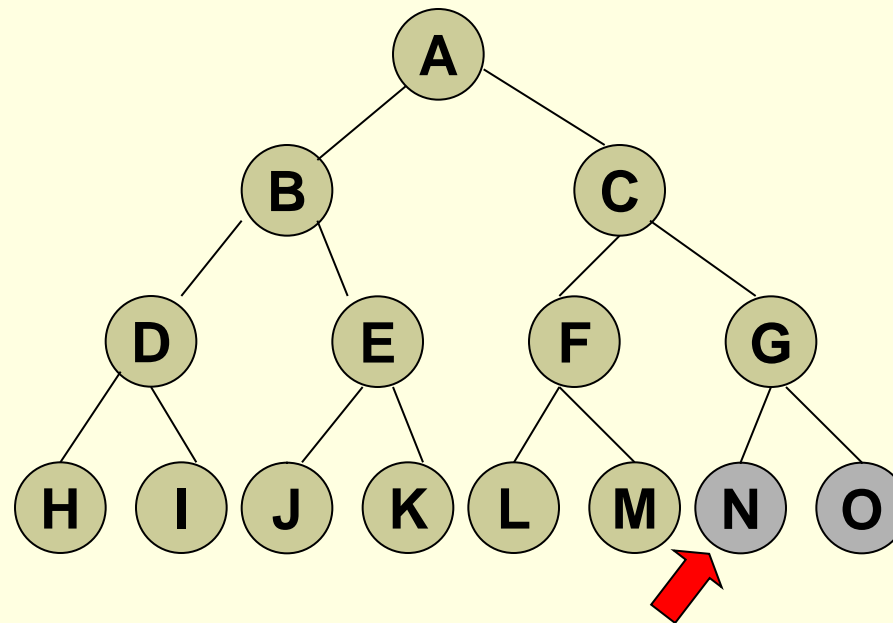
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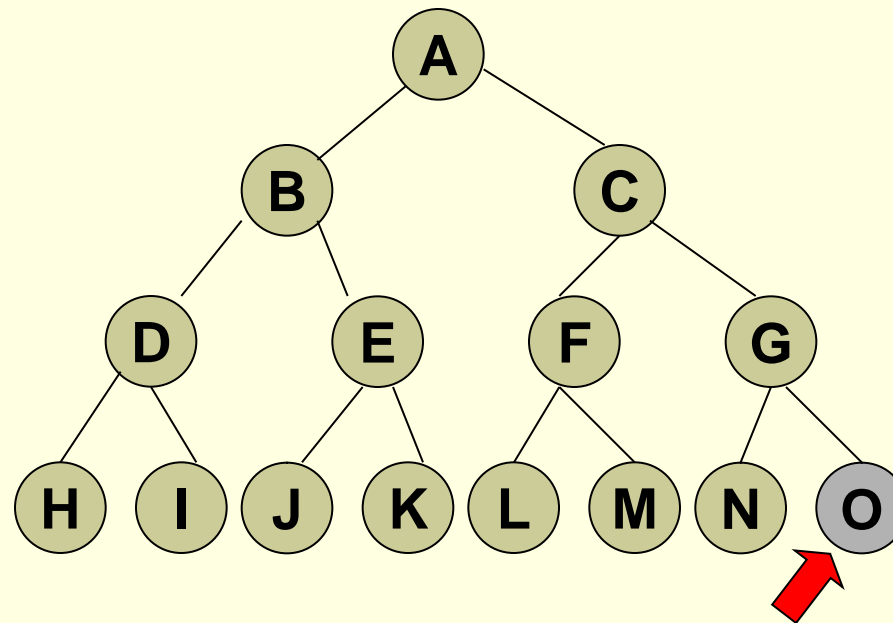
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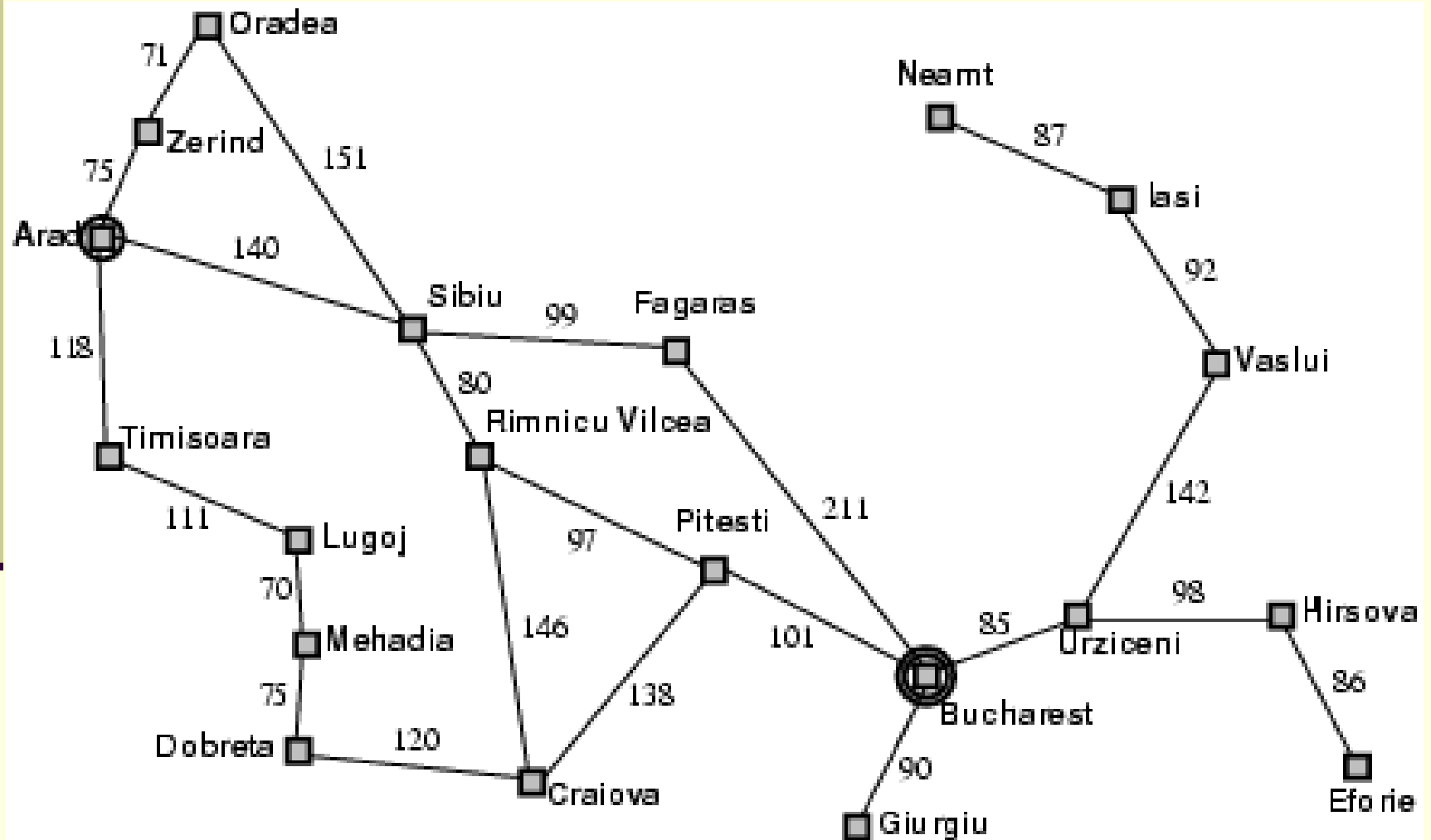
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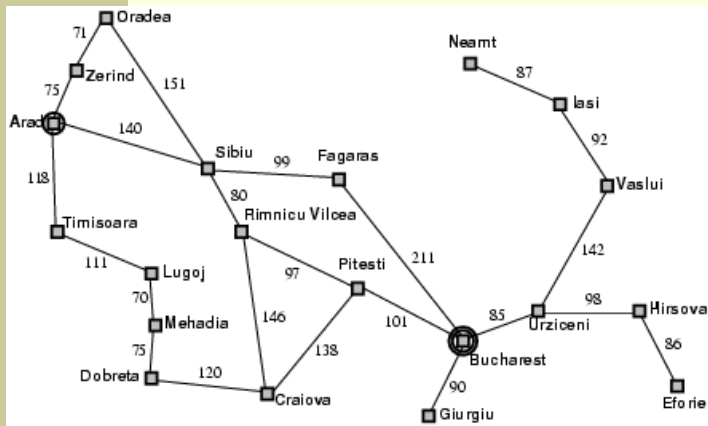
Problema de rutare: un agent *american*

- Vacanta in Romania – in Arad.
- In ziua urmatoare ii pleaca avionul din Bucuresti.
- **Formulara scopului:**
 - Ajungerea in Bucuresti
- **Formulara problemei:**
 - **Stari:** diverse orase
 - **Actiuni:** de a merge dintr-un oras in altul
- **Gasirea solutiei:**
 - O secventa de orase, de ex: Arad, Sibiu, Fagaras, Bucuresti.

Un agent *american*



Algoritm cautare in latime



functia *cautare_latime*(problema) **intoarce** solutie sau **esec**
 noduri = genereaza_coada(genereaza_nod(stare_initiala[problema]))

Cat timp este posibil *executa*

Daca noduri = vida *atunci*

intoarce **esec**

nod = scoate_din_fata(noduri)

Daca testare_tinta[problema] se aplica la stare(nod) *atunci*

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Altfel

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Sfarsit *cat timp*

Arad

Fața

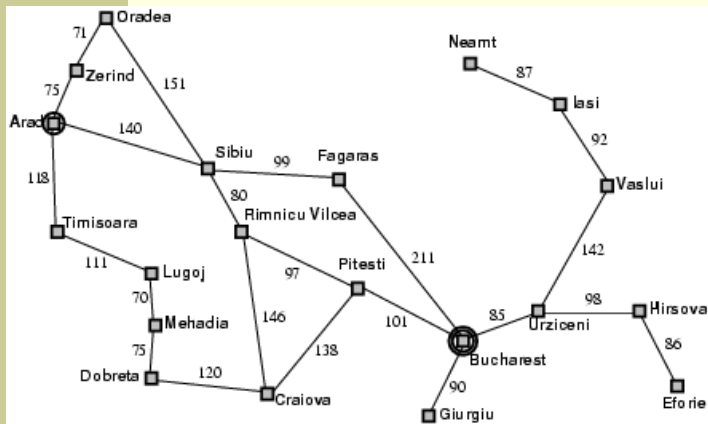
noduri

Sfarsit

Arad

Parcurgerea: Arad,

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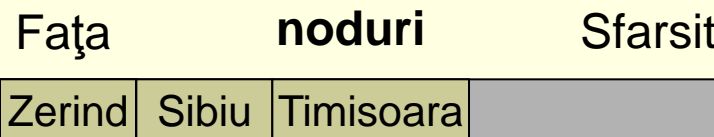
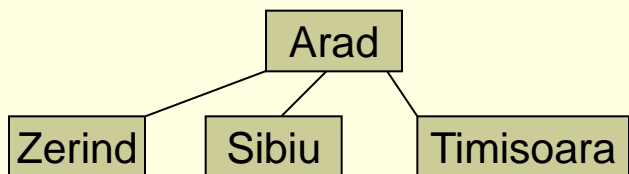
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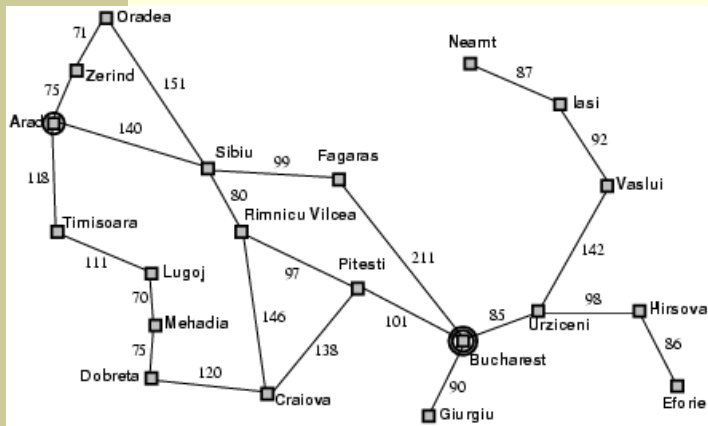
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Sfarsit cat timp



Parcurgerea: Arad, Zerind

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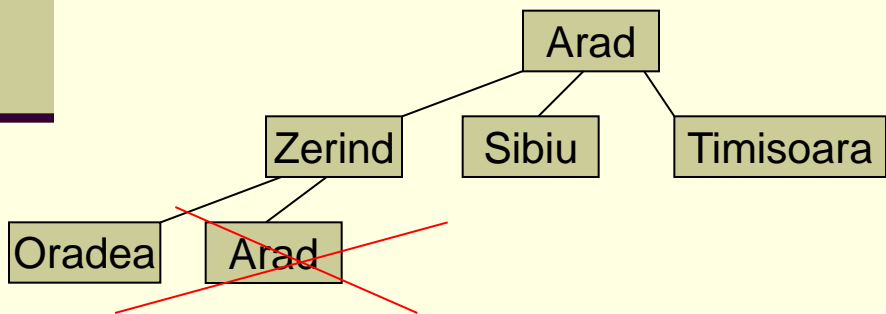
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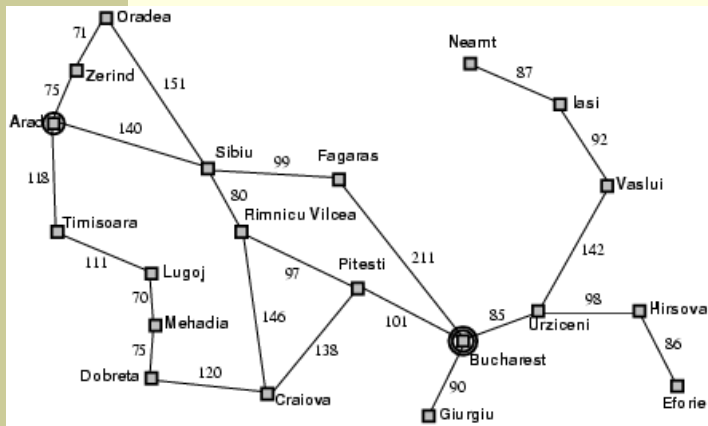


Fața	noduri	Sfarsit
Zerind	Sibiu	Timisoara

Parcurgerea: Arad, Zerind

A mai aparut acest nod!

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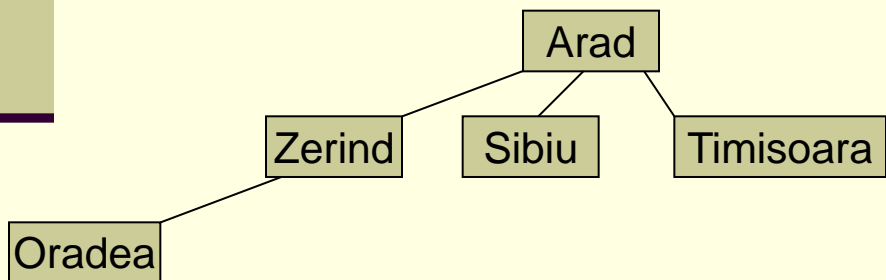
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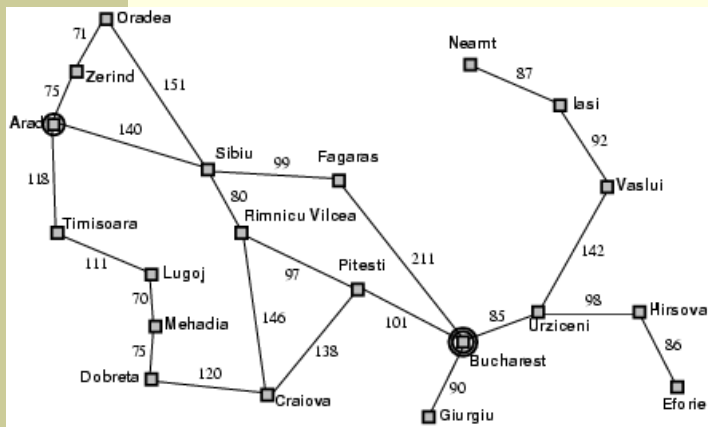
Sfarsit cat timp



Fața	noduri			Sfarsit
Sibiu	Timisoara	Oradea		

Parcurgerea: Arad, Zerind, Sibiu

Algoritm cautare in latime



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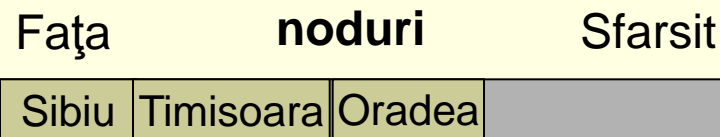
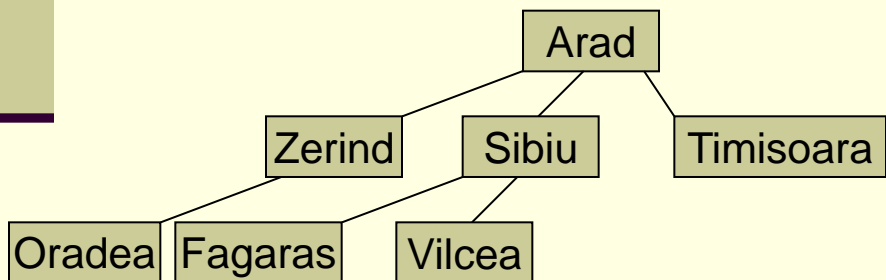
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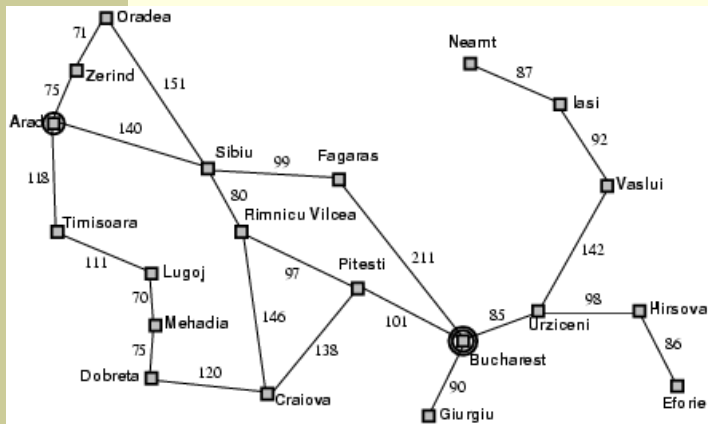
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Sfarsit cat timp



Parcurgerea: Arad, Zerind, Sibiu

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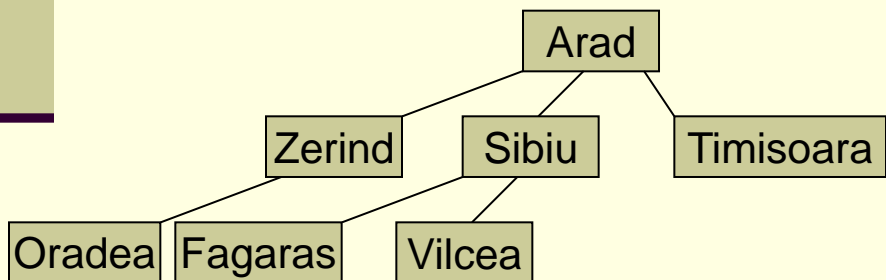
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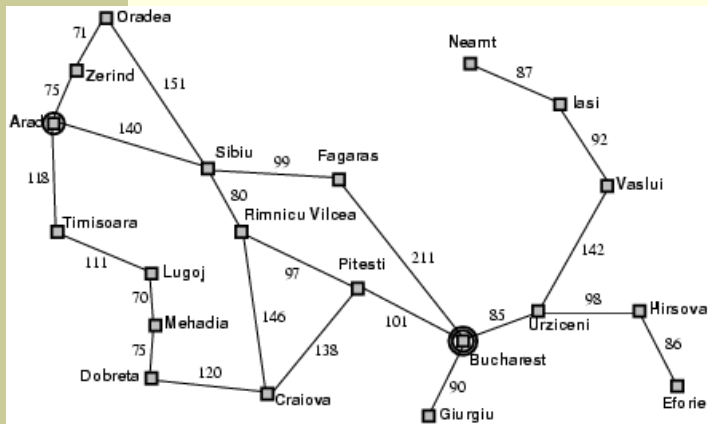
Sfarsit cat timp



Fața	noduri	Sfarsit
Timisoara	Oradea	

Parcurgerea: Arad, Zerind, Sibiu, Timisoara

Algoritm cautare in latime



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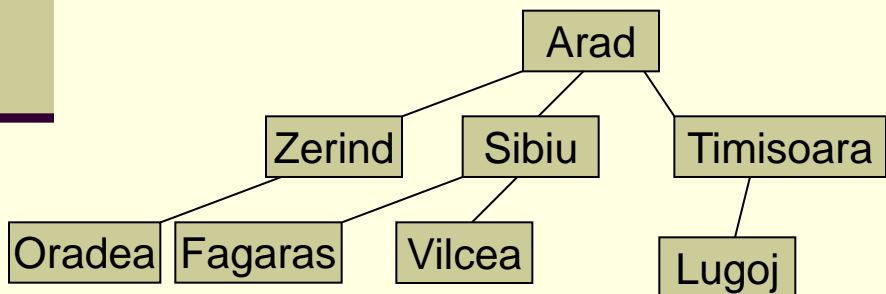
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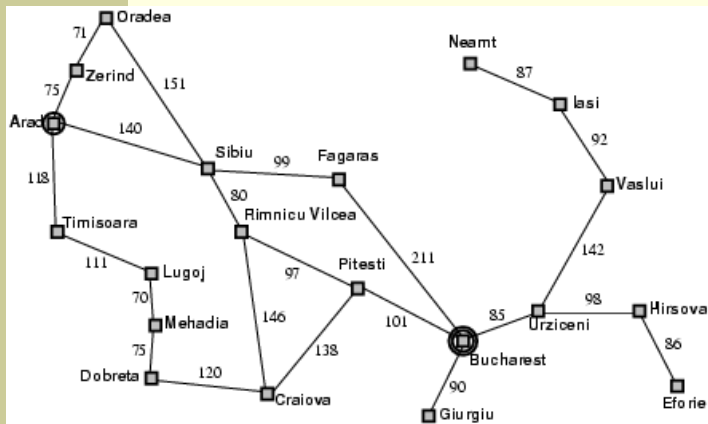
Sfarsit cat timp



Fața	noduri	Sfarsit
Timisoara	Oradea Fagaras Vilcea	

Parcurgerea: Arad, Zerind, Sibiu, Timisoara

Algoritm cautare in latime



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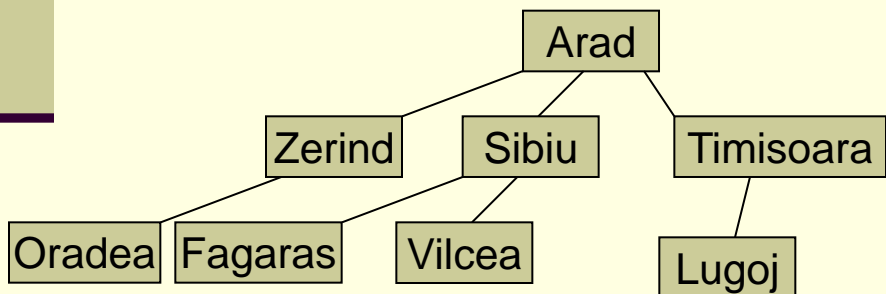
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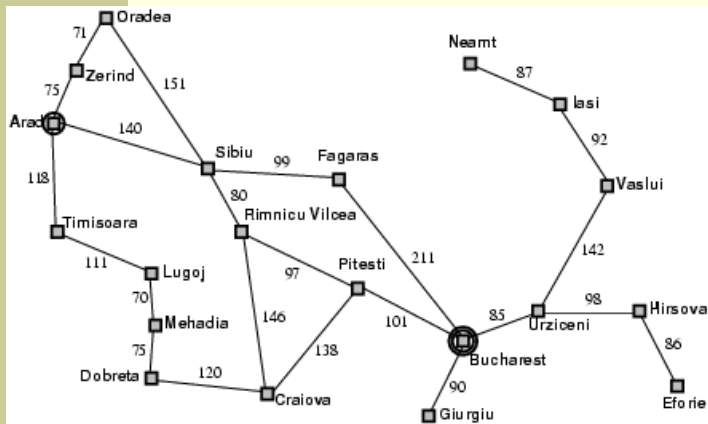
Sfarsit *cat timp*



Fața	noduri	Sfarsit		
Oradea	Fagaras	Vilcea	Lugoj	

Parcurgerea: Arad, Zerind, Sibiu, Timisoara, Oradea

Algoritm cautare in latime



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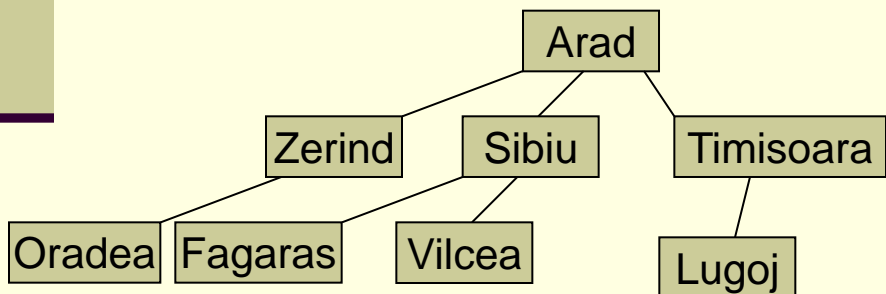
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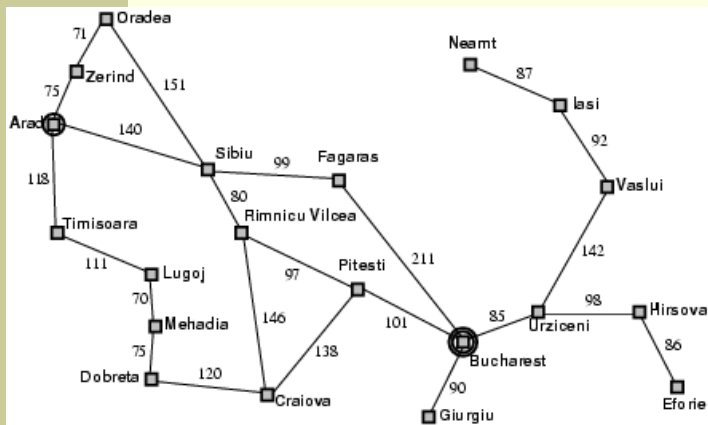
Sfarsit cat timp



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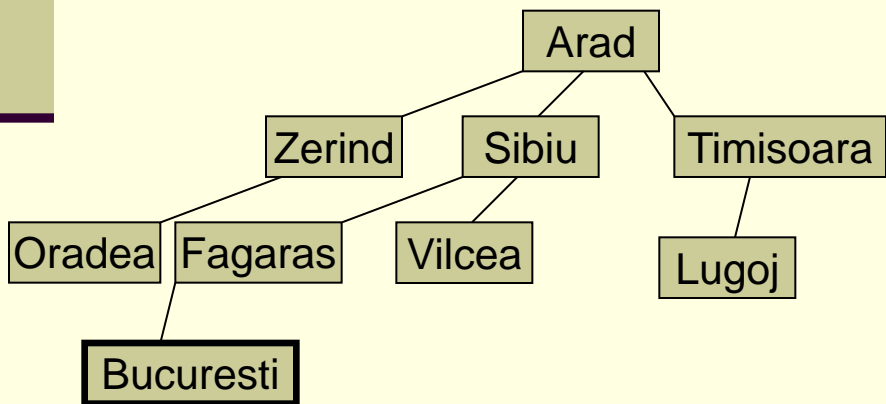
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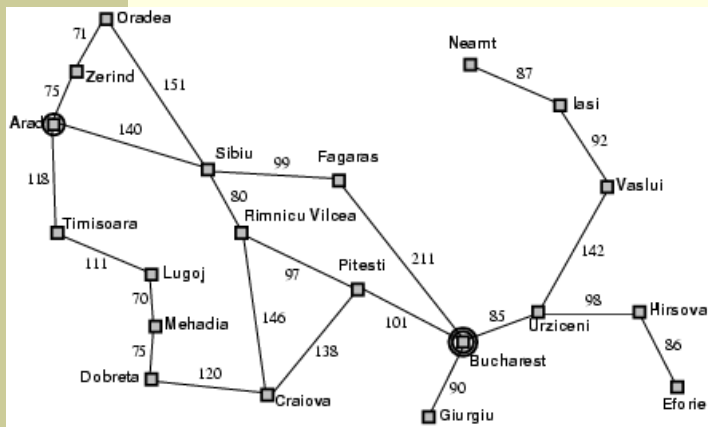
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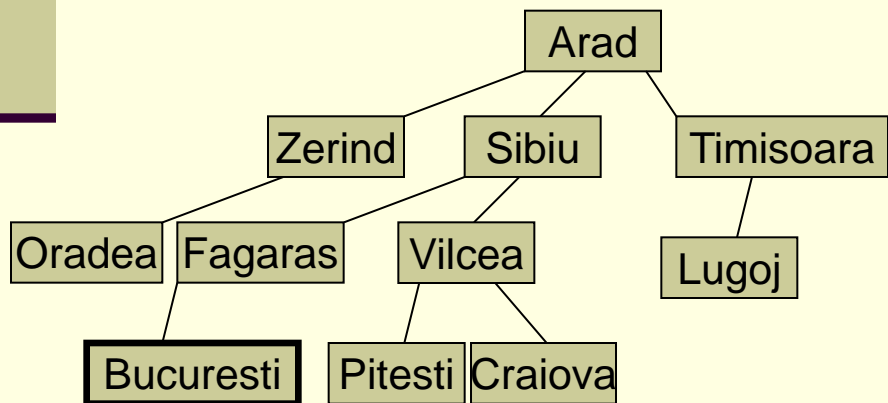
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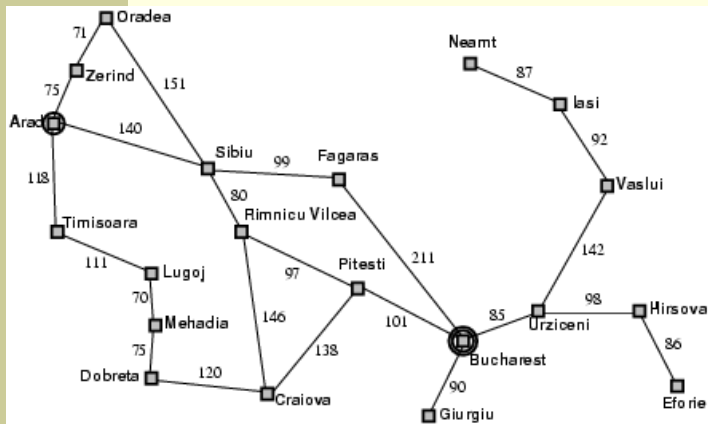
Sfarsit *cat timp*



Fața	noduri	Sfarsit
Vilcea	Lugoj	Bucuresti

Parcurgerea: Arad, Zerind, Sibiu, Timisoara, Oradea, Fagaras, Vilcea

Algoritm cautare in latime



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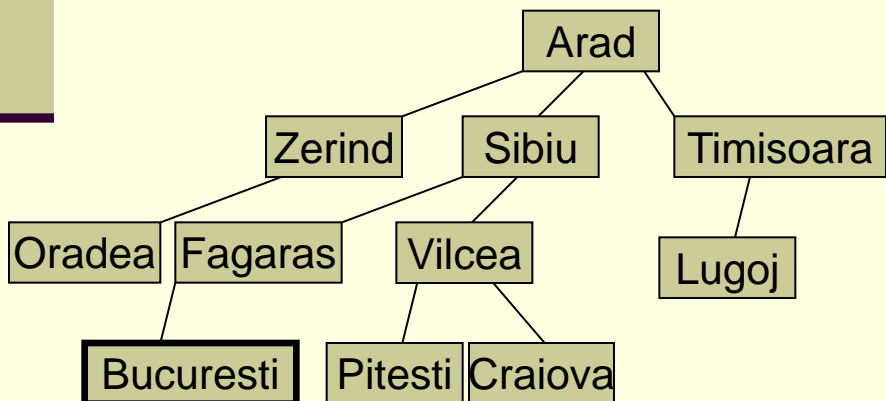
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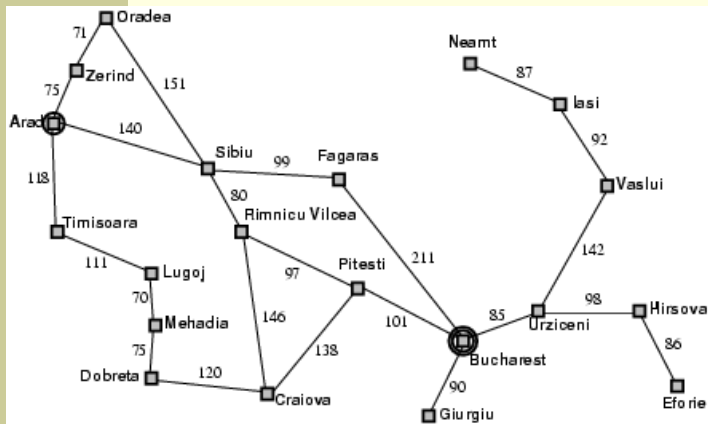
Sfarsit cat timp



Fața	noduri	Sfarsit
Lugoj	Bucuresti	Pitesti
Craiova		

Parcurgerea: Arad, Zerind, Sibiu, Timisoara, Oradea, Fagaras, Vilcea, Lugoj

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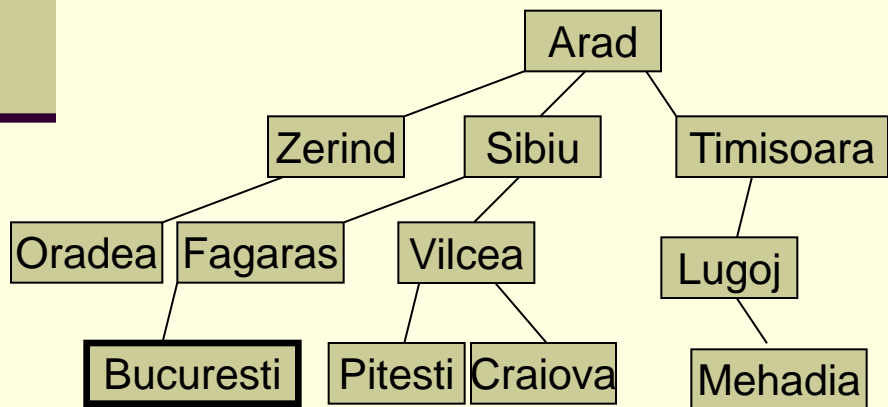
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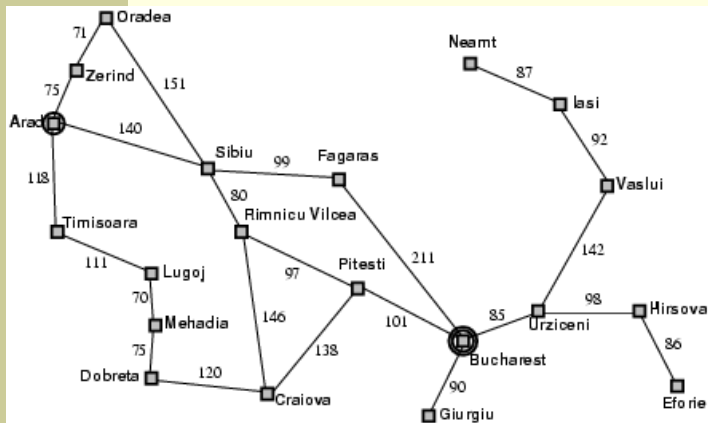
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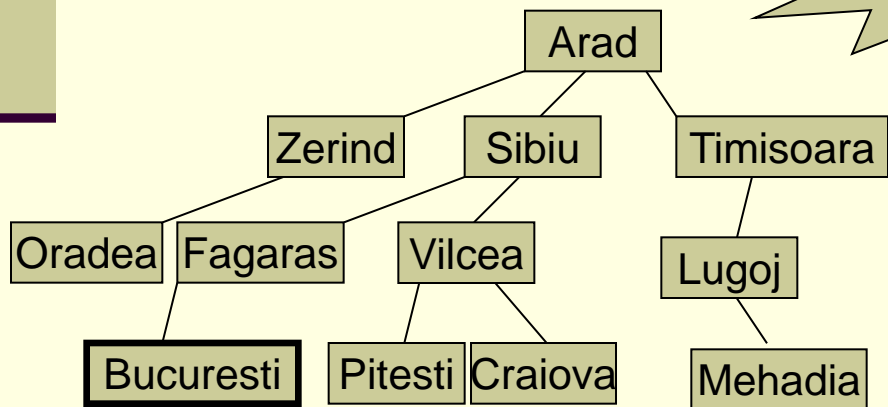
intoarce nod

Altfel

noduri = adauga(noduri, expandare(nod, adauga_la_sfarsit))

Sfarsit ca

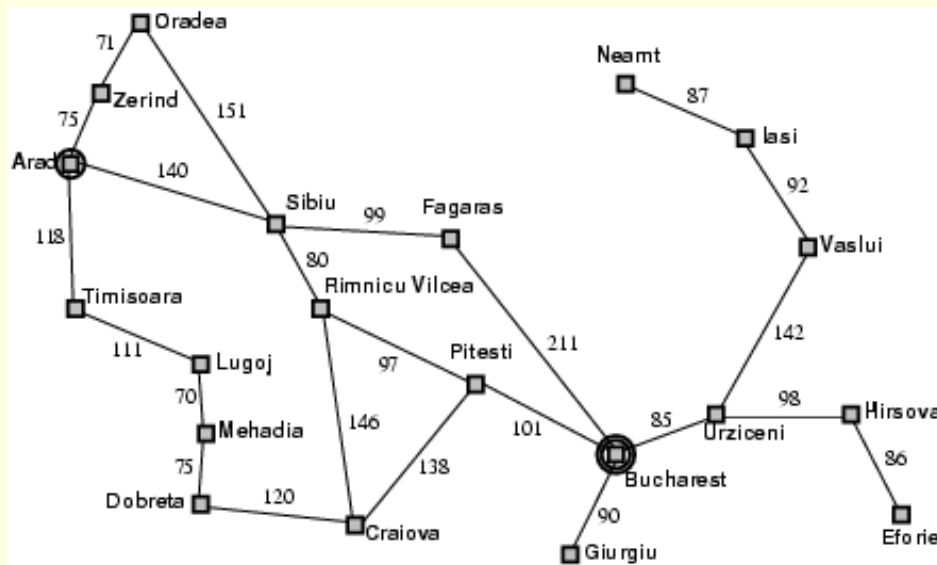
Nod tinta!



Fața	noduri	Sfarsit
	Bucuresti	Pitesti Craiova Mehadia

Parcurgerea: Arad, Zerind, Sibiu, Timisoara, Oradea, Fagaras, Vilcea, Lugoj, **Bucuresti!**

Exercitiu



Fața **noduri** Sfarsit



Gasiti o ruta de la Bucuresti la Sibiu folosind parcurgerea in latime.

Desenati arborele, scrieti parcurgerea si continutul pentru noduri la fiecare pas.

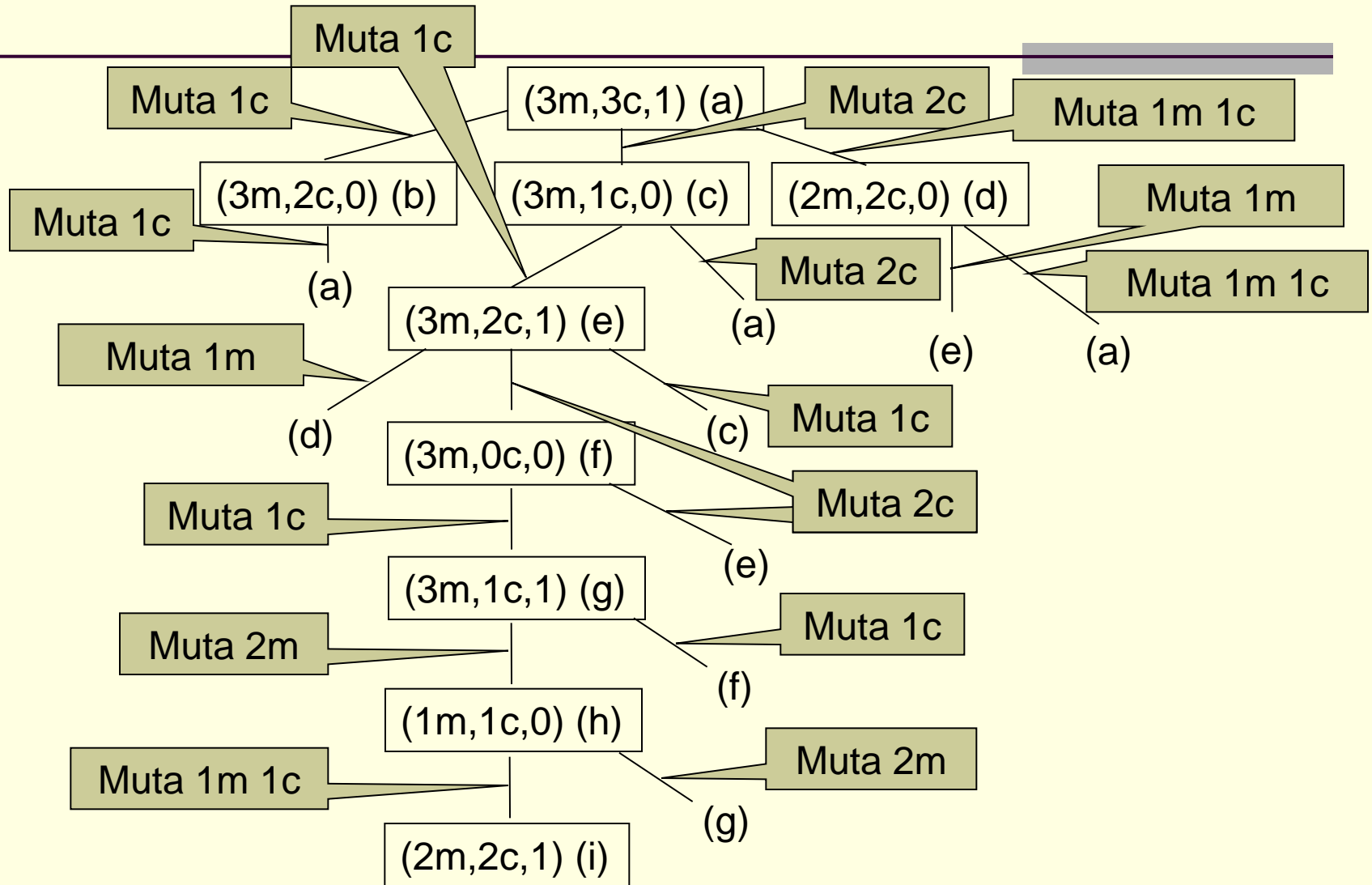
Parcurgerea: Bucuresti, ..., Rm. Vilcea

Misionarii si canibalii

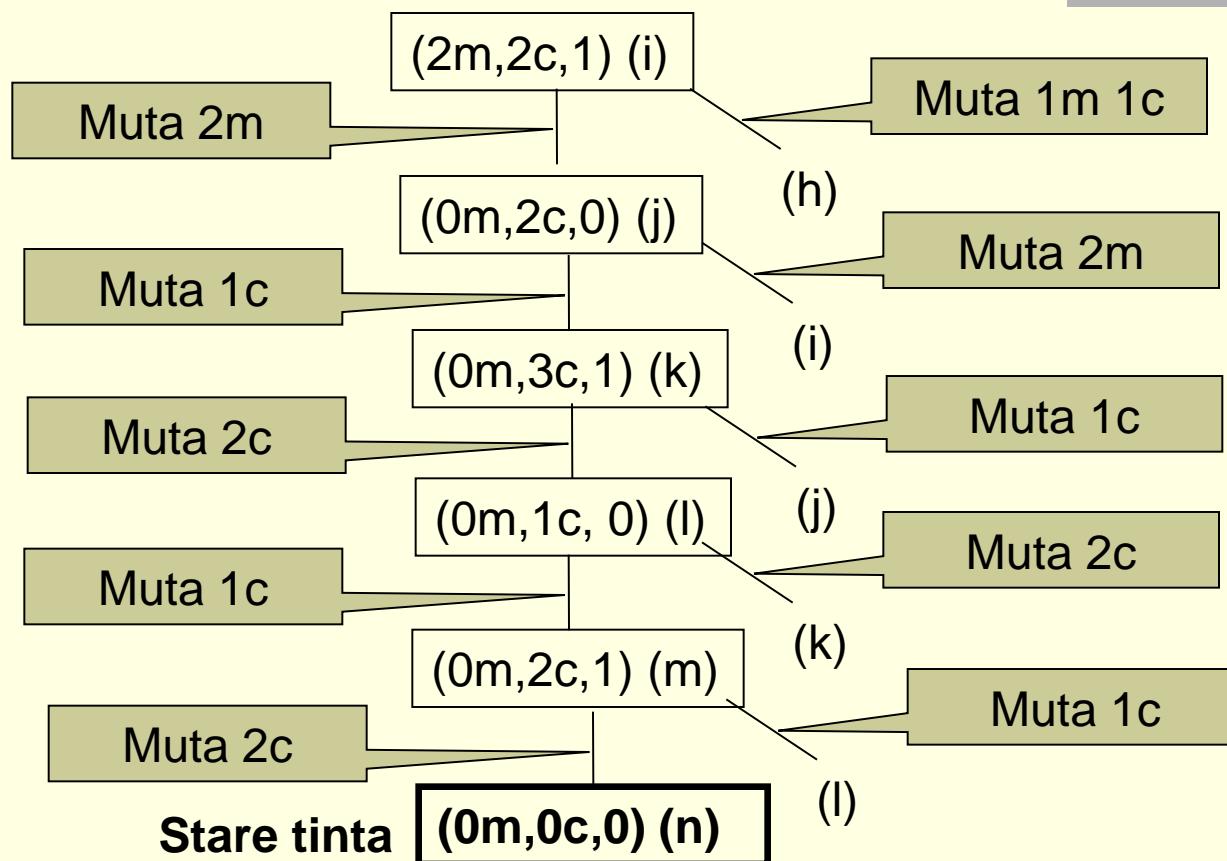


- Trei misionari si trei canibali se afla de o parte a raului. Ei au o barca ce poate duce cel mult doi oameni. Gasiti o posibilitate sa traverseze toti de cealalta parte a raului cu conditia sa nu existe mai multi canibali decat misionari intr-o parte.
- **Stari:** secvente ordonate de 3 numere reprezentand numarul de misionari, canibali si barci de partea in care se aflau initial (3, 3, 1).
- **Actiuni:** mutarea unui misionar sau canibal sau 2 canibali, 2 misionari sau un misionar si un canibal de pe o parte pe alta.
- **Testarea tintei:** starea (0, 0, 0).
- **Costul drumului:** numarul de traversari.

Misionarii si canibalii



Misionarii si canibalii



Puzzle cu 8 valori

	2	3
1	4	6
7	5	8

Starea initiala

1	2	3
4	5	6
7	8	

Starea tinta

- **Stari:** este descrisa locatia fiecarei cifre in una din cele 9 casute.
- **Actiuni:** casuta goala se misca la stanga, dreapta, sus sau jos.
- **Testarea tintei:** starea se gaseste in configuratia din dreapta.
- **Costul drumului:** fiecare pas are costul 1, deci costul drumului este dat de numarul de mutari.

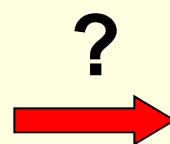
Puzzle cu 15 valori

- Sam Loyd a introdus în 1878 15-puzzle-ul.
- A oferit un premiu de 1 000 \$ din proprii bani pentru cel care rezolva problema în situația în care doar 14 și 15 sunt inversate, restul fiind aliniate crescător.



Puzzle cu 15 valori

1	2	3	4
5	6	7	8
9	10	11	12
13	15	14	



1	2	3	4
5	6	7	8
9	10	11	12
13	14	15	

Nimeni nu a castigat premiul!

Puzzle cu 8 valori

- Cate stari posibile exista?
 - $9! = 362\,880$ stari
- Numai la **jumatate** din aceste stari se poate ajunge din orice stare data.

Posibilitatea de a atinge scopul final...

- O valoare j apare dupa o valoare i daca
 - j apare pe acelasi rand, dar in dreapta lui i
 - j se afla sub linia lui i
- Pentru $i = 1, 2, \dots, 8$, fie n_i numarul de aparitii ale lui j ($j < i$) dupa i .
- $N = n_2 + n_3 + \dots + n_8$

	2	3
1	4	6
7	5	8

$$n_2 = 1$$

$$n_6 = 1$$

$$n_3 = 1$$

$$n_7 = 1$$

$$n_4 = 0$$

$$n_8 = 0$$

$$n_5 = 0$$

$$N = 4$$

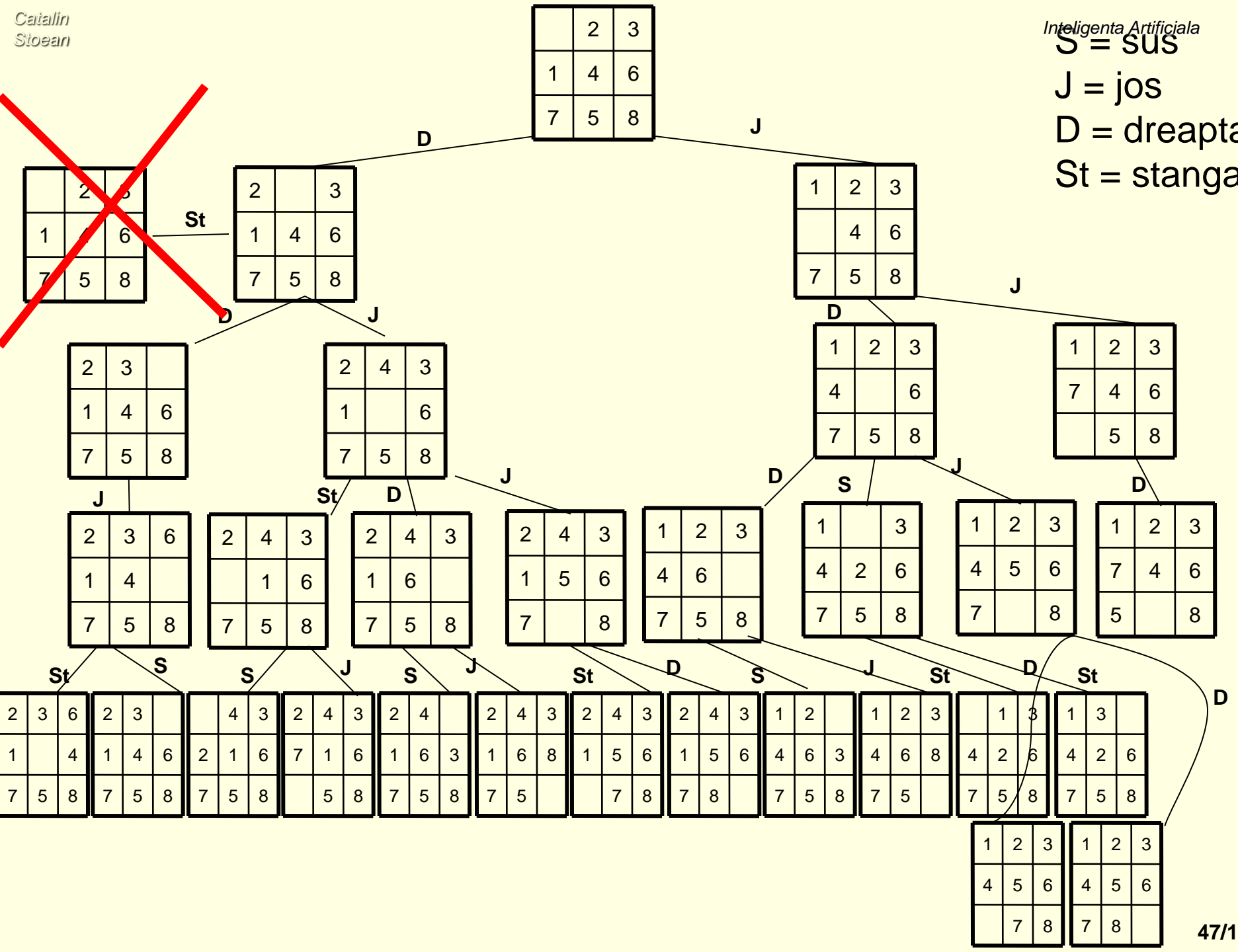
Pentru N par, puzzle-ul cu 8 valori este rezolvabil!

S = sus

J = jos

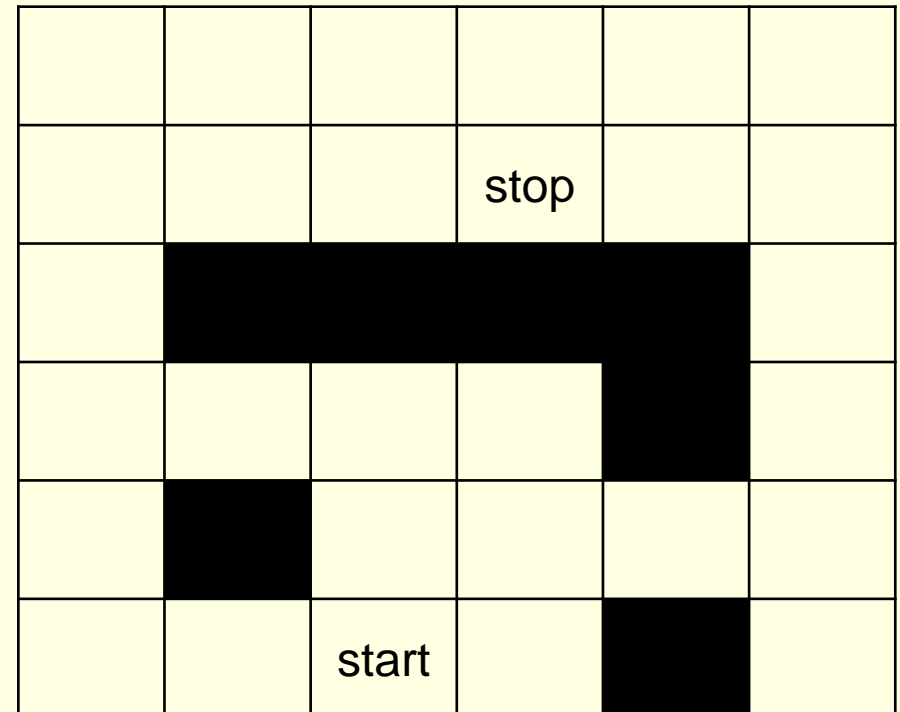
D = dreapta

St = stanga



Exercitiu

- Considerăm problema găsirii unei rute în figura de mai jos de la start la stop.
- Agentul se mută un pătrat la fiecare pas vertical sau orizontal.
- Nu se poate deplasa în pătratele hasurate.
- Etichetați cu litere în ordine alfabetică pătratele dacă se utilizează o căutare în adâncime, iar ordinea operațiilor este: sus, stânga, dreapta și jos.



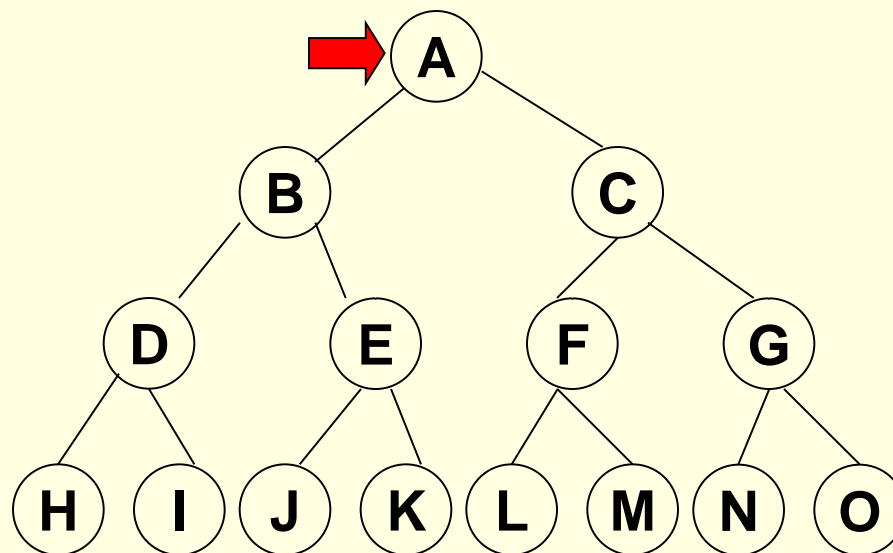
Exercitiu - Problema celor 4 dame

- **Stari:** orice aranjament de 0 pana la 4 dame care nu se ataca.
- **Actiuni:** adauga o dama pe coloana cea mai din stanga a.i. sa nu fie atacata de alta dama.
- **Testarea tintei:** 4 dame care nu se ataca pe tabla.
- **Costul drumului:** 0.

- Pornind de la o tabla de 4x4 goala si folosind datele problemei de mai sus, sa se construiasca printr-o cautare in latime arborele complet care duce la rezolvarea problemei. Numerotati nodurile in ordinea in care au fost vizitate.

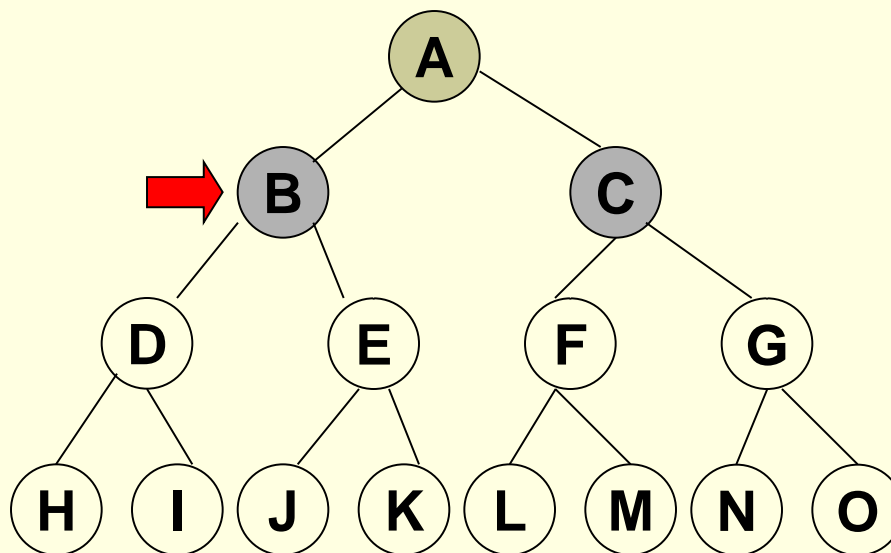
Cautarea in adancime

- Se expandeaza nodul radacina, apoi se merge pe un drum pana se ajunge la cel mai adanc nivel al arborelui.
- Numai cand se ajunge la final (la nodurile frunza), cautarea se intoarce si expandeaza noduri de la nivelele mai putin adanci.



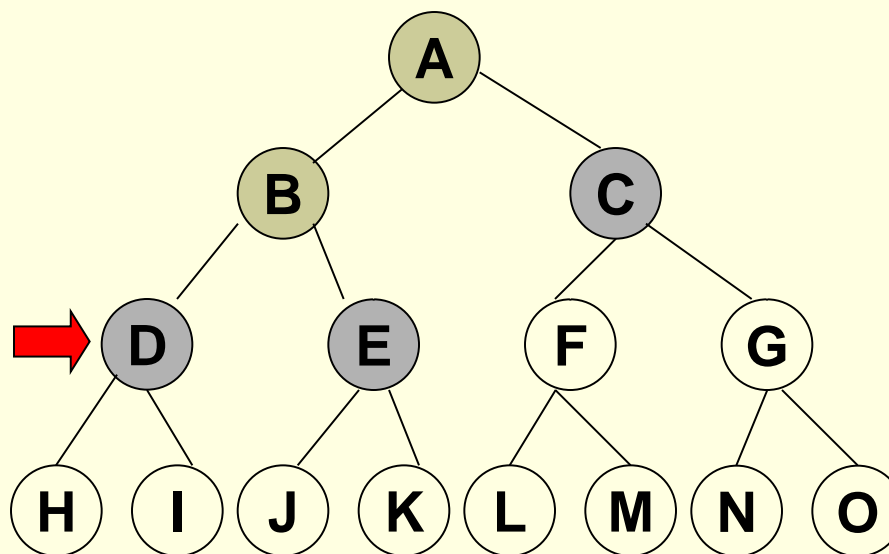
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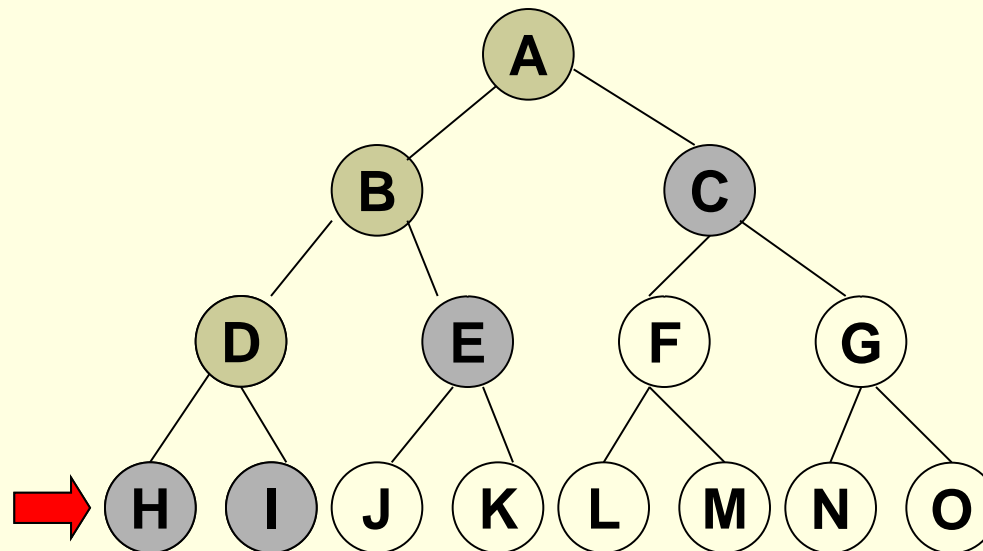
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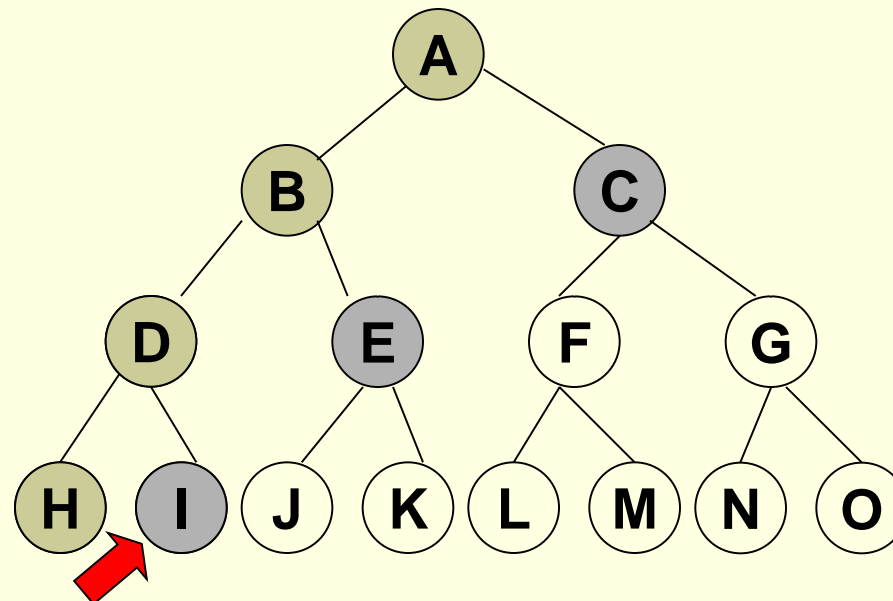
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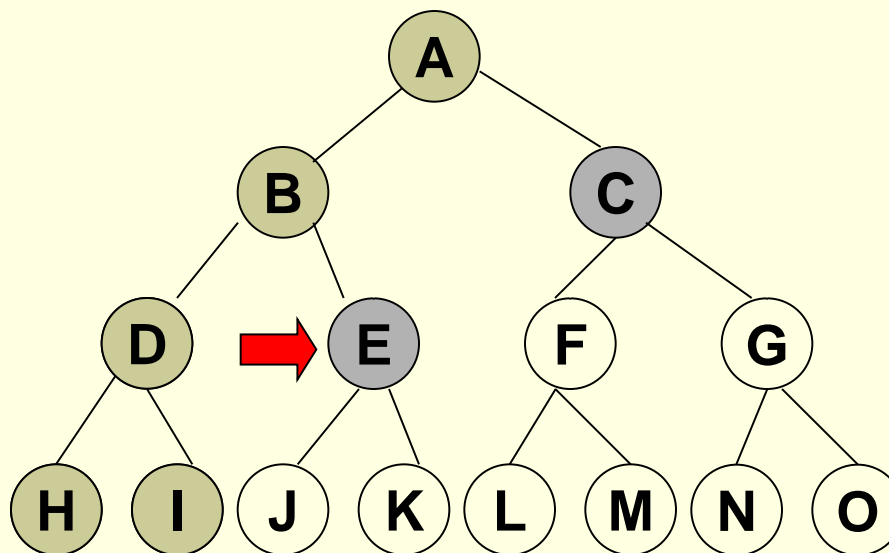
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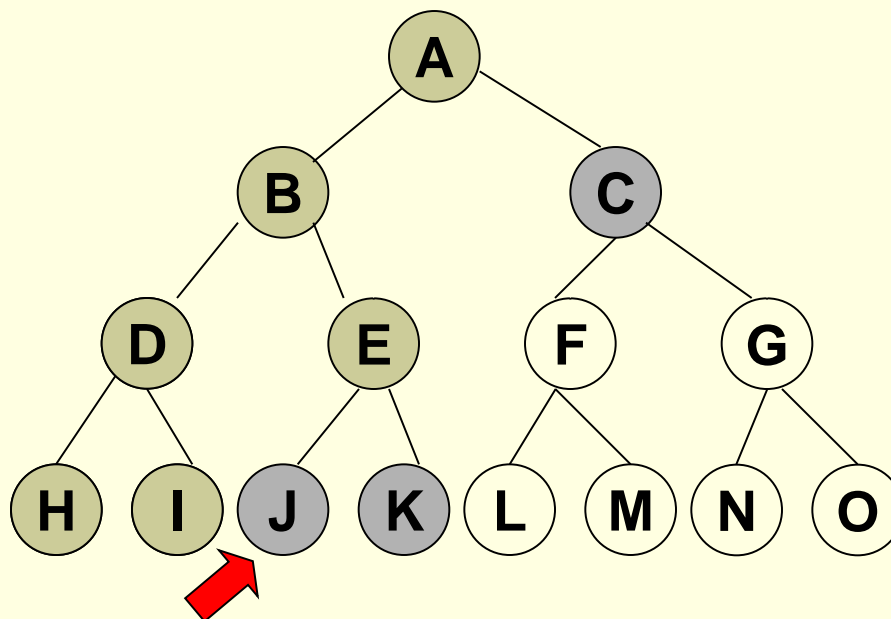
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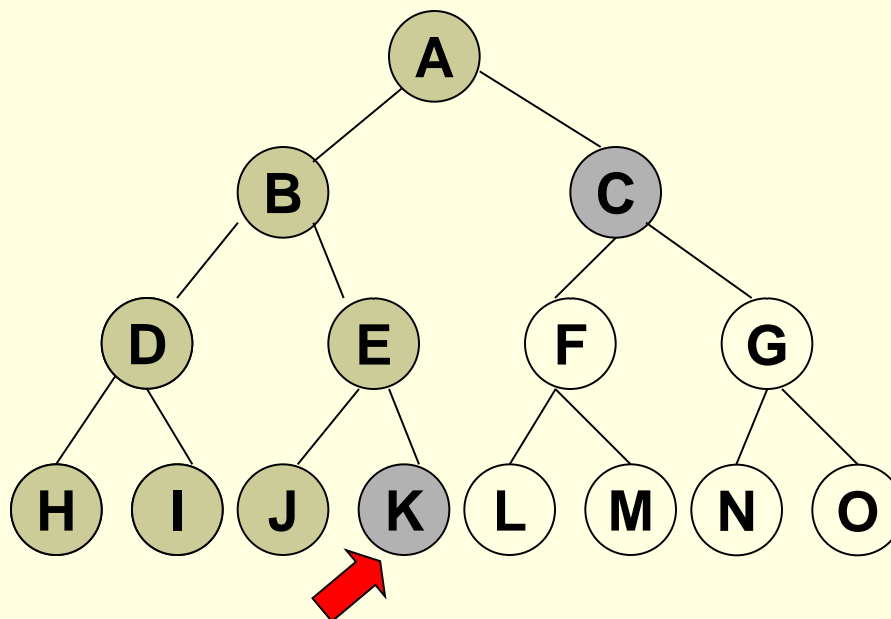
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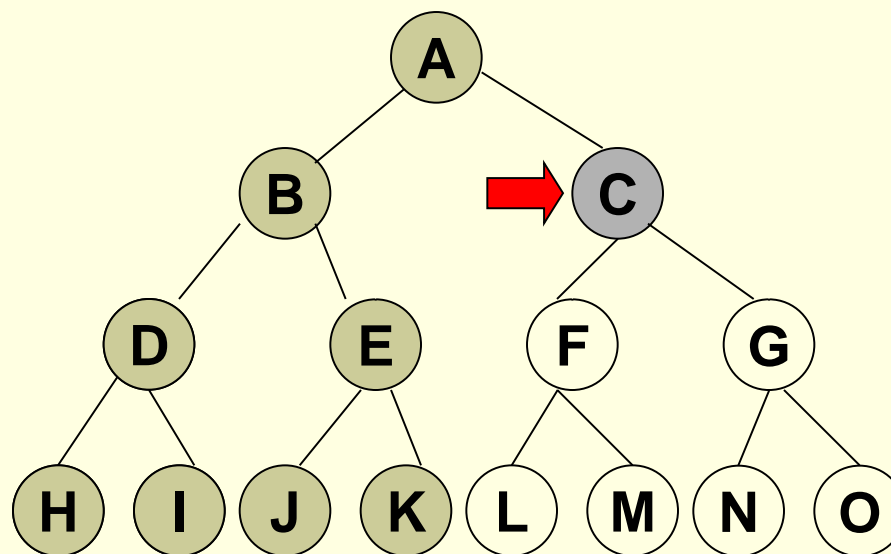
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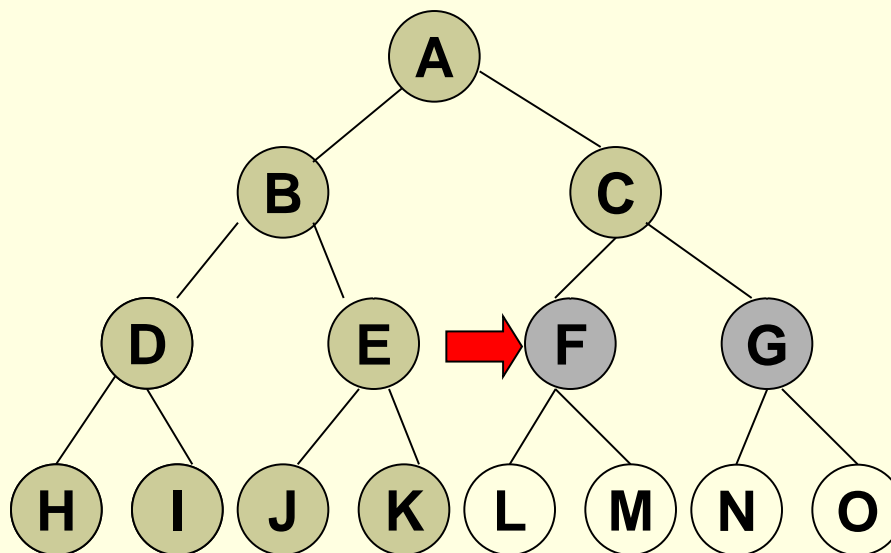
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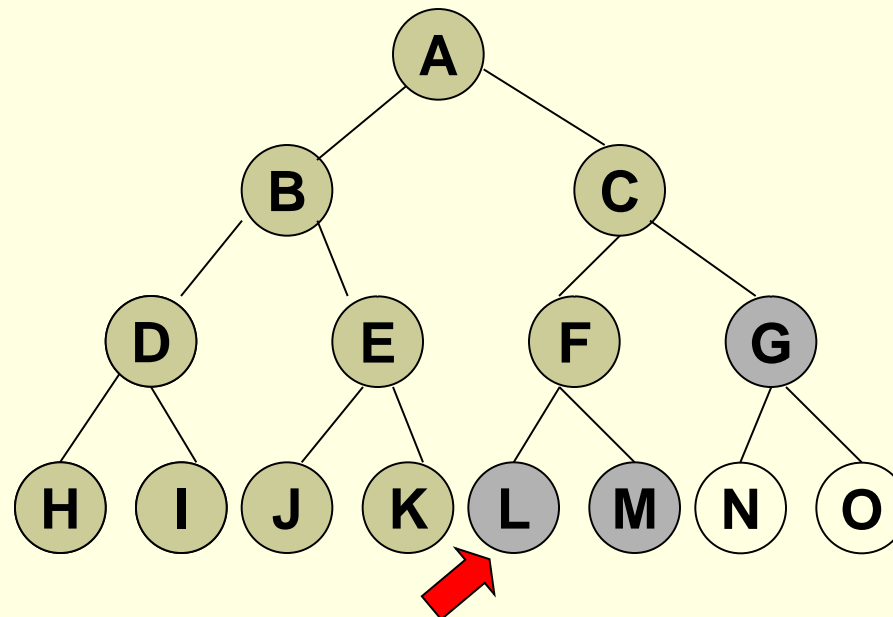
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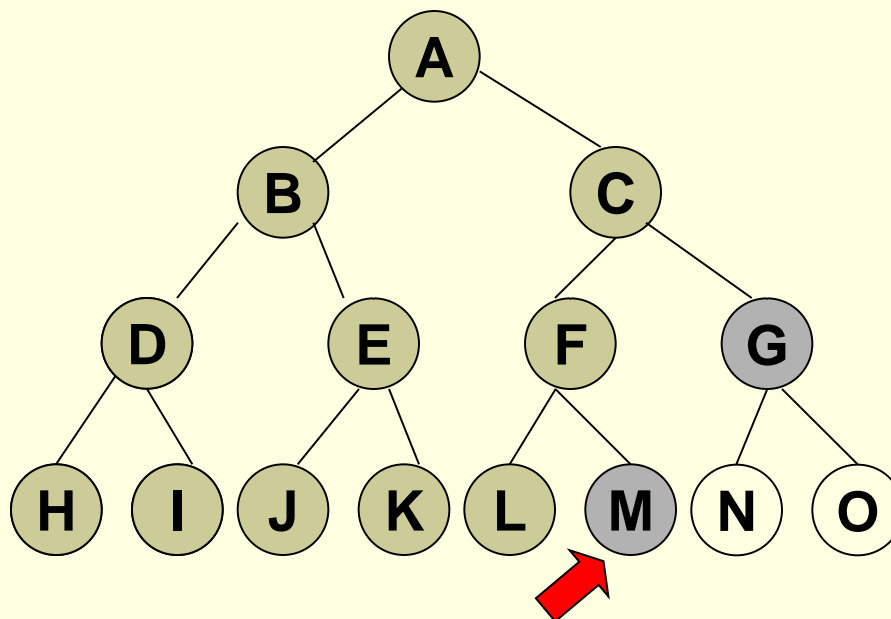
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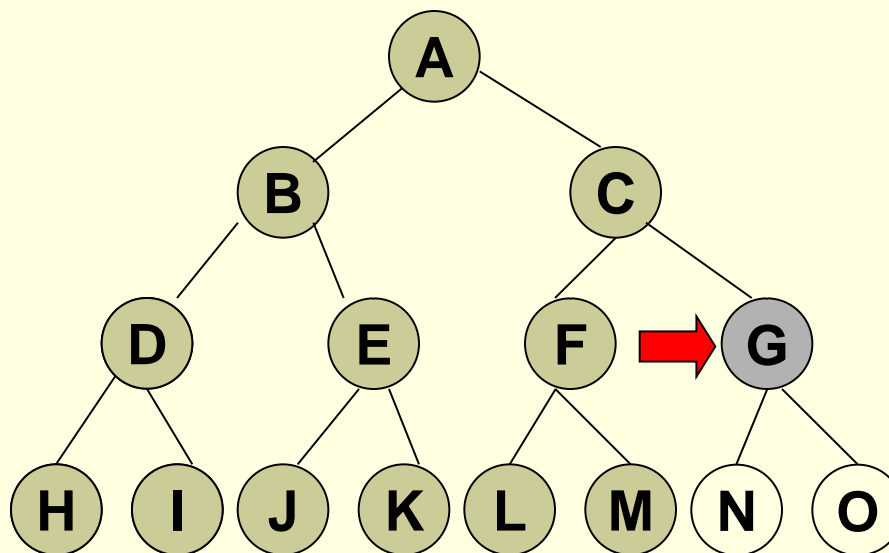
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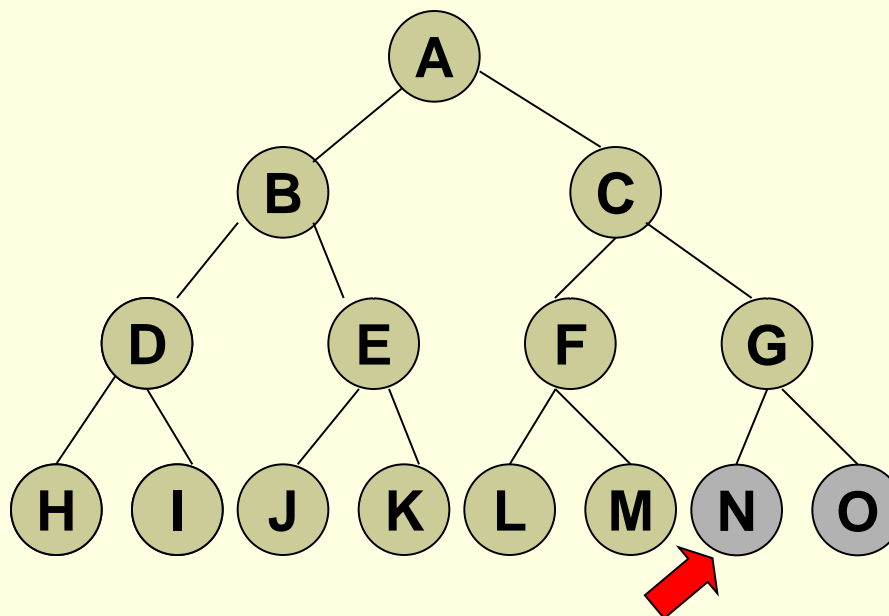
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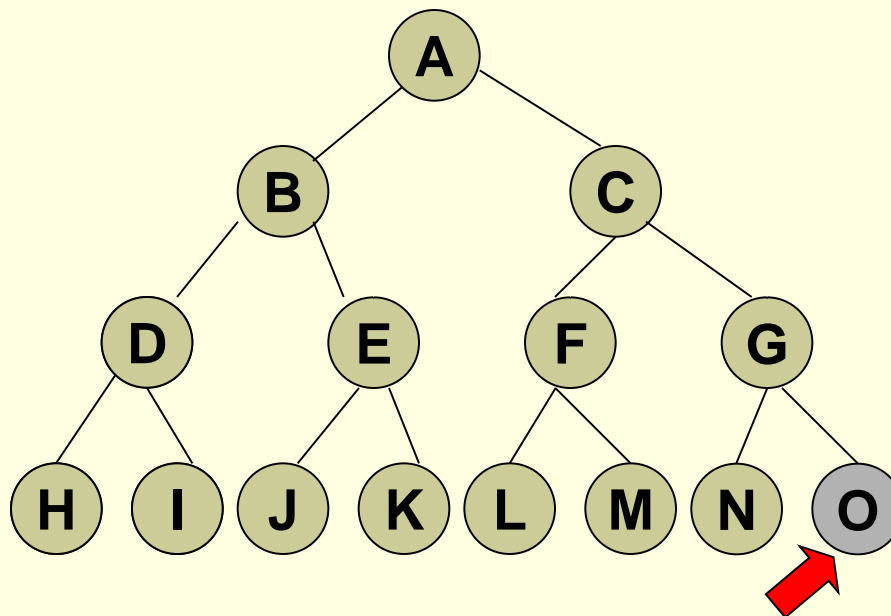
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Parcurgerea in adancime: A, B, D, H, I, E, J, K, C, F, L, M, G, N, O.

Algoritm cautarea in adancime

functia cautare_adancime(problema) **intoarce** solutie sau esec
noduri = genereaza_coadă(genereaza_nod(stare_initiala[problema]))

Cat timp este posibil executa

Daca noduri = vida atunci

intoarce esec

nod = scoate_din_fata(noduri)

Daca testare_tinta[problema] se aplica la stare(nod) atunci

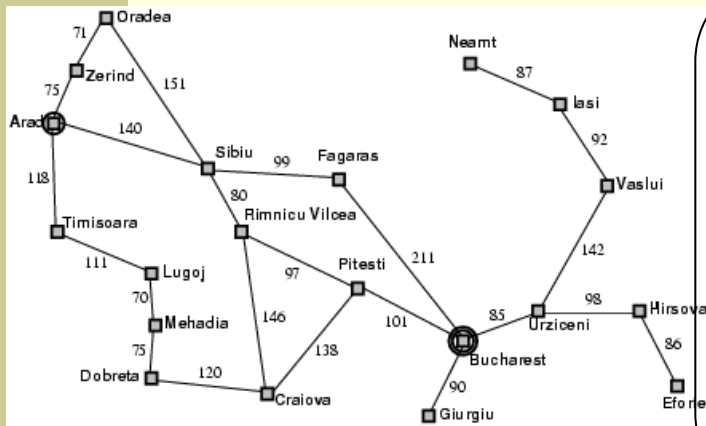
intoarce nod

Altfel

noduri = adauga(noduri, expandare(nod, adauga_la_inceput))

Sfarsit cat timp

Algoritm cautare in adancime



Arad

```

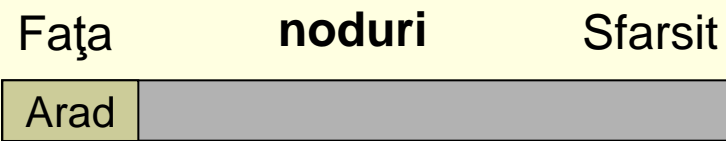
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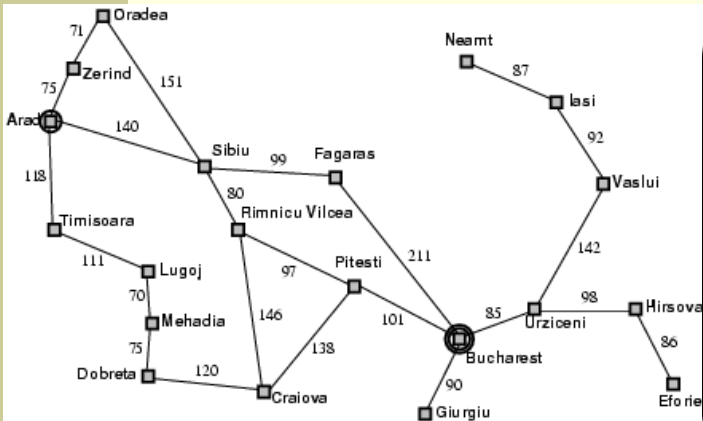
Sfarsit cat timp

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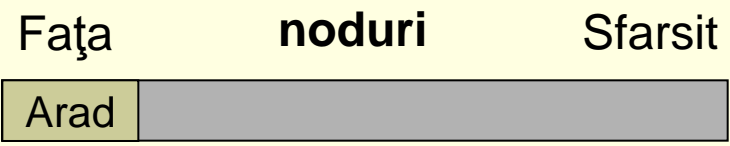
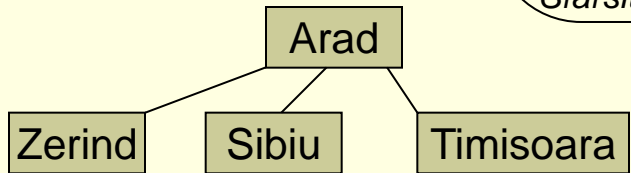


Parcurgerea: Arad,

Algoritm cautare in adancime

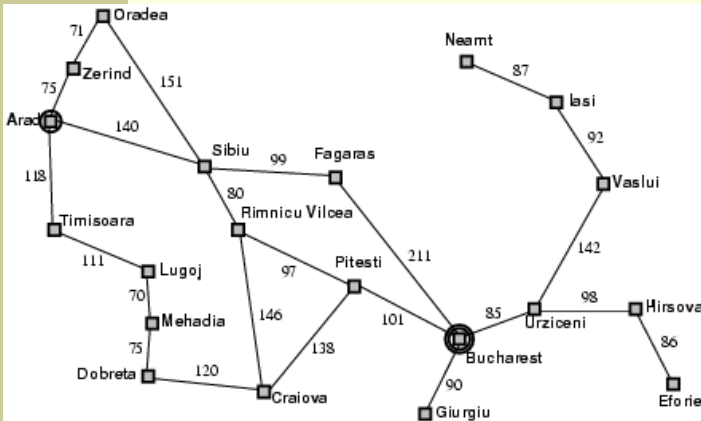


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intoarce `nod`
Altfel
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Sfarsit cat timp



Parcurgerea: Arad,

Algoritm cautare in adancime



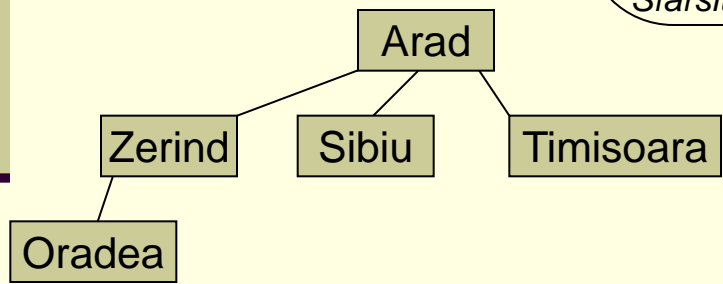
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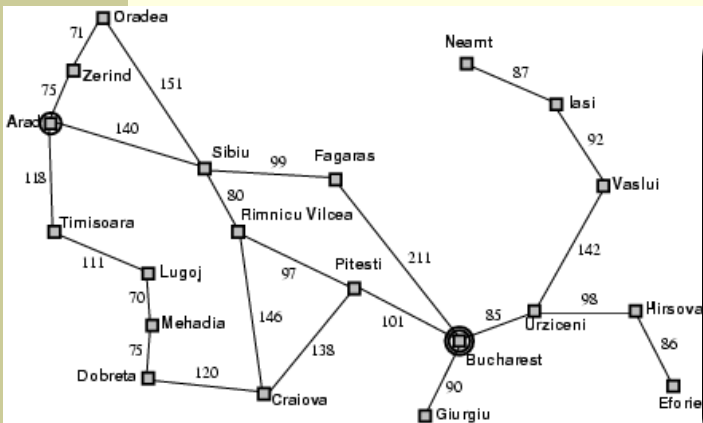
Sfarsit cat timp



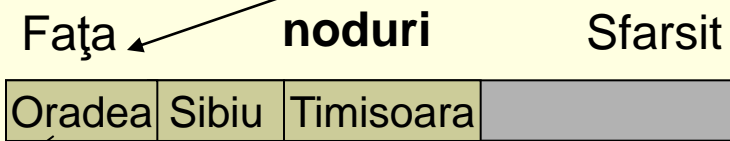
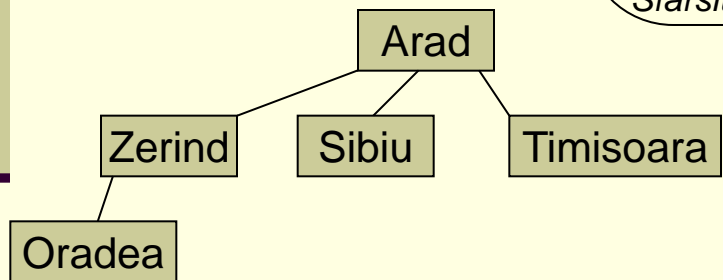
Fața	noduri	Sfarsit	
Zerind	Sibiu	Timisoara	

Parcurgerea: Arad, Zerind,

Algoritm cautare in adancime



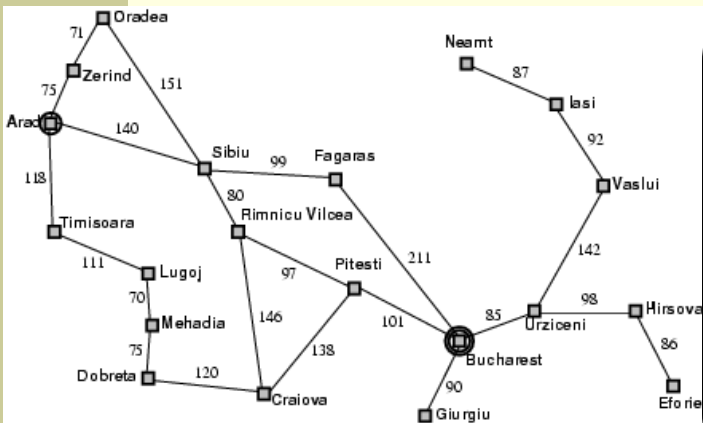
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 Sfarsit cat timp



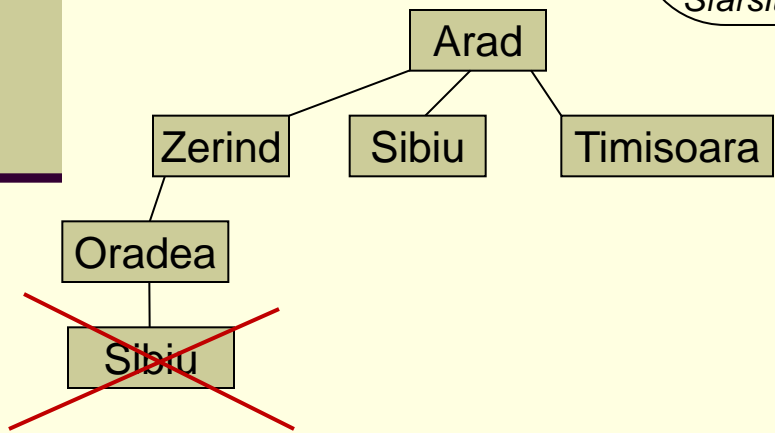
Parcurgerea: Arad, Zerind,

Adaugarea se face prin față!

Algoritm cautare in adancime



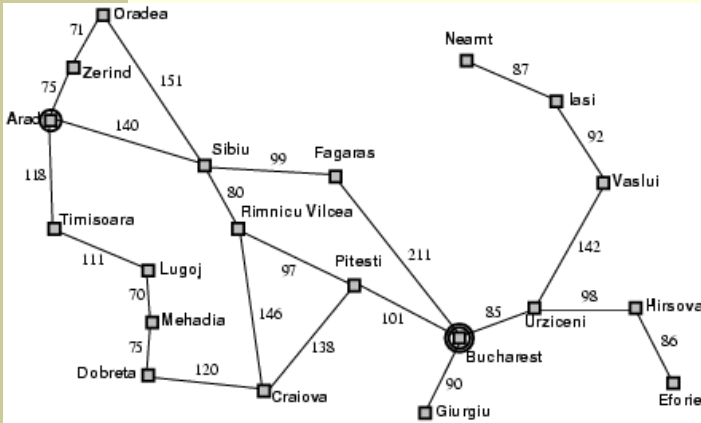
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Sfarsit cat timp



Fața	noduri	Sfarsit
Oradea	Sibiu	Timisoara

Parcurgerea: Arad, Zerind, Oradea

Algoritm cautare in adancime



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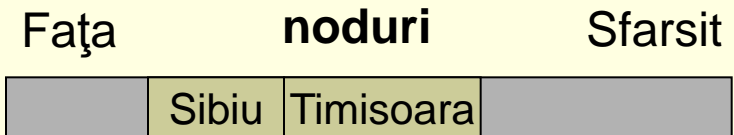
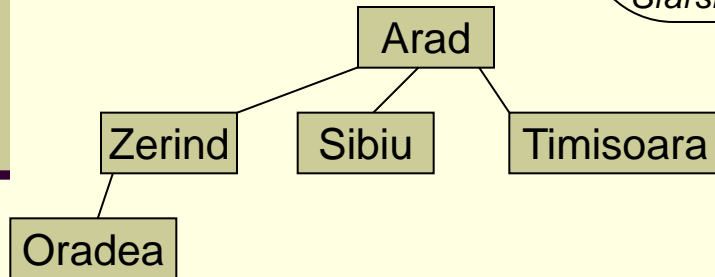
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Altfel

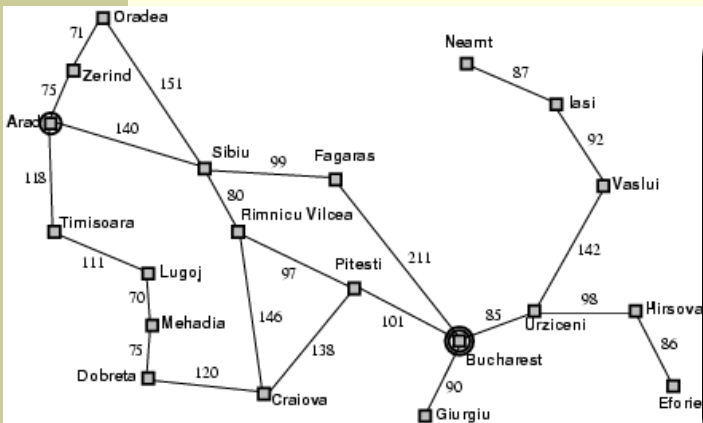
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Sfarsit cat timp



Parcurgerea: Arad, Zerind, Oradea, Sibiu

Algoritm cautare in adancime



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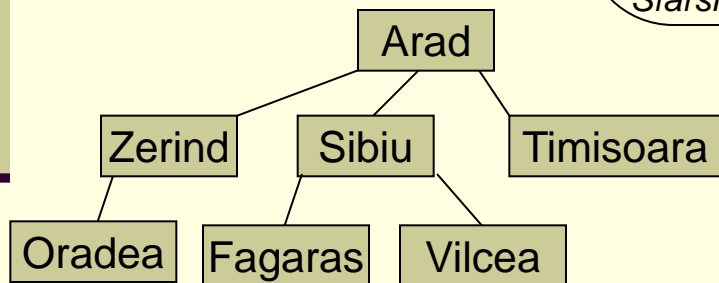
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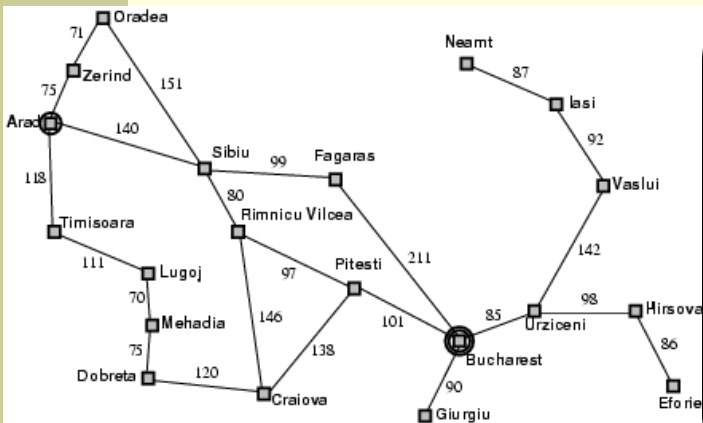
Sfarsit cat timp



Fața	noduri	Sfarsit
Fagaras	Vilcea	Timisoara

Parcurgerea: Arad, Zerind, Oradea, Sibiu

Algoritm cautare in adancime



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nod = scoate_din_fata(noduri)

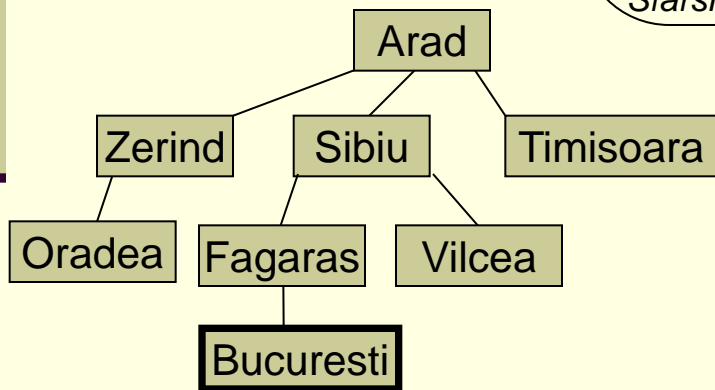
Daca testare_tinta[problema] se aplica la stare(nod) atunci

intoarce nod

Altfel

noduri = adauga(noduri, expandare(nod, adauga_la_inceput))

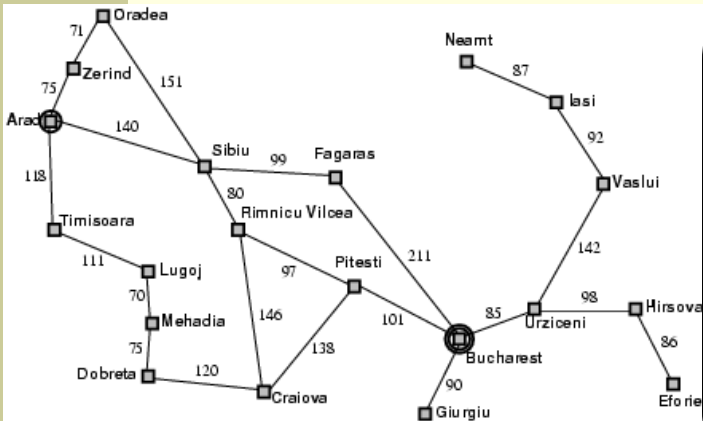
Sfarsit cat timp



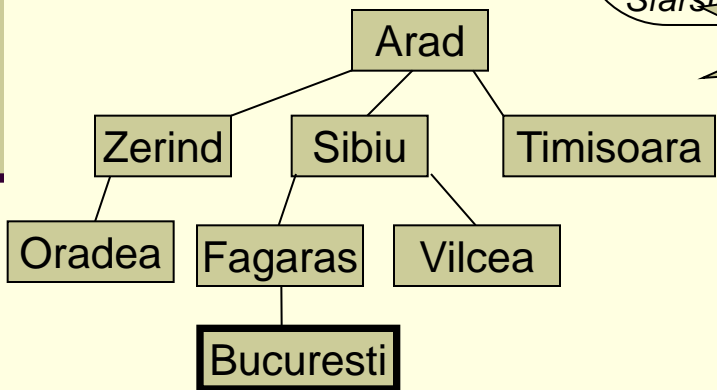
Fața	noduri	Sfarsit
Fagaras	Vilcea	Timisoara

Parcurgerea: Arad, Zerind, Oradea, Sibiu, Fagaras

Algoritm cautare in adancime



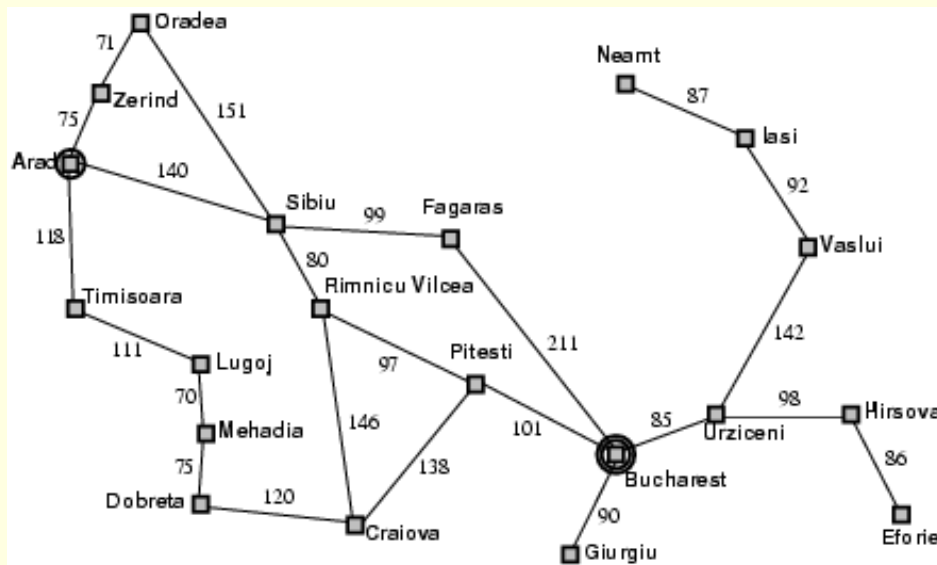
functia cautare_adancime(problema) **intoarce** solutie sau esec
 noduri = genereaza_coada(genereaza_nod(stare_initala[problema]))
 Cat timp este posibil executa
 Daca noduri = vida atunci
 intoarce esec
 nod = scoate_din_fata(noduri)
 Daca testare_tinta[problema] se aplica la stare(nod) atunci
 intoarce nod
 Altfel
 noduri = dauga(noduri, expandare(nod, adauga_la_inceput))
 Sfarsit



Fața	noduri	Sfarsit
	Bucuresti Vilcea Timisoara	

Parcurgerea: Arad, Zerind, Oradea, Sibiu, Fagaras, Bucuresti

Exercitiu



Fața

noduri

Sfarsit

Gasiti o ruta de la Timisoara la Vaslui folosind parcurgerea in adancime. Desenati arborele, scrieti parcurgerea si continutul pentru noduri la fiecare pas.

Parcurgerea: Timisoara, ..., Vaslui

Exercitiu - Problema celor 4 dame

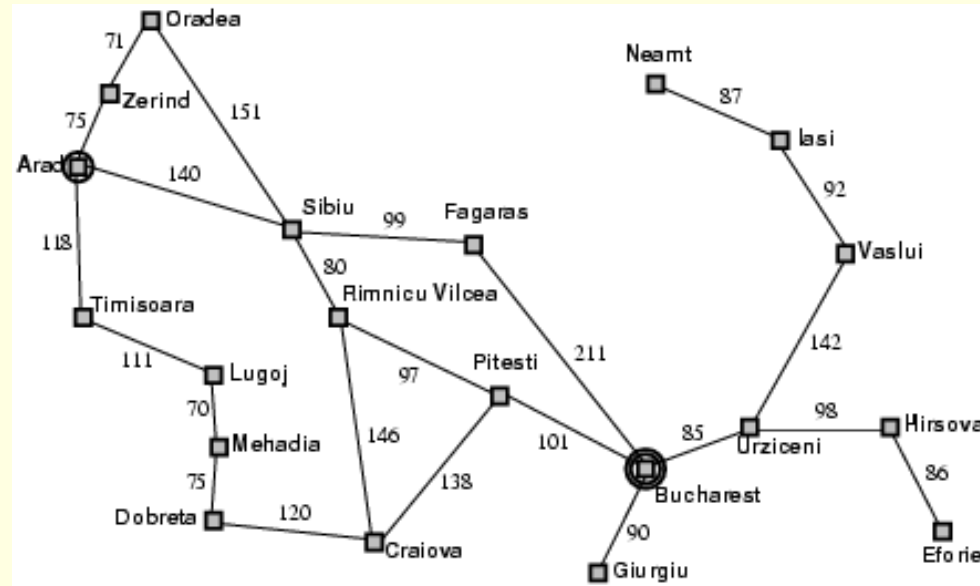
- **Stari:** orice aranjament de 0 pana la 4 dame care nu se ataca.
- **Actiuni:** adauga o dama pe coloana cea mai din stanga a.i. sa nu fie atacata de alta dama.
- **Testarea tintei:** 4 dame care nu se ataca pe tabla.
- **Costul drumului:** 0.

- Pornind de la o tabla de 4x4 goala si folosind datele problemei de mai sus, sa se construiasca printr-o cautare in adancime arborele complet care duce la rezolvarea problemei. Numerotati nodurile in ordinea in care au fost vizitate.

Cautarea limitata in adancime

- Impune o margine superioara pentru lungimea unui drum.
- Se poate utiliza la probleme unde stim la ce adancime maxima trebuie sa gasim solutia
 - Ex: avem 20 de orase, ne aflam in orasul A, solutia trebuie sa se gaseasca la maxim 19 pasi.
- Daca l este limita de adancime stabilita, atunci complexitatile:
 - Pentru timp: $O(b^l)$
 - Pentru spatiu: $O(bl)$.

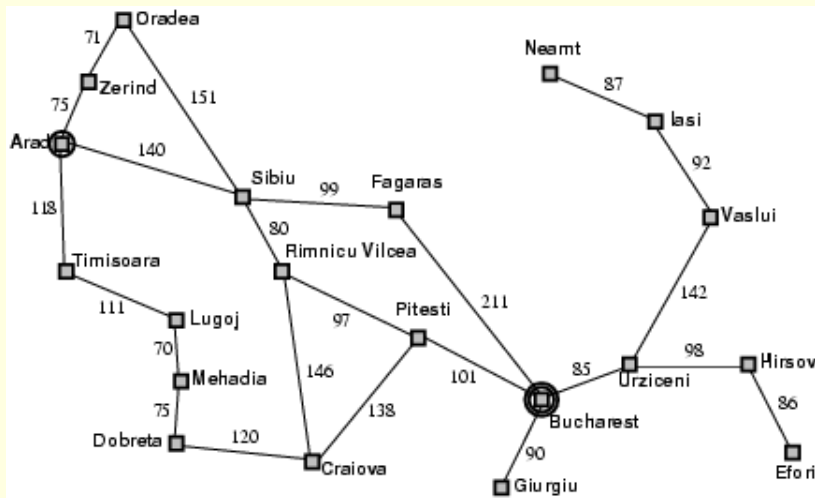
Cautarea limitata in adancime



Stabilim limita de adancime egala cu 3.

Sa se gaseasca o ruta de la Arad la Bucuresti folosind cautarea limitata in adancime.

Cautarea limitata in adancime



Arad

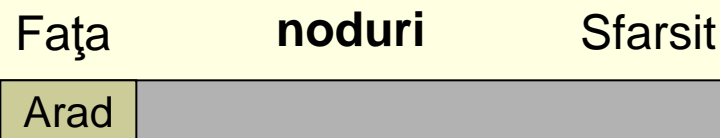
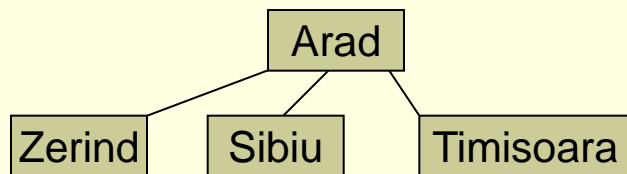
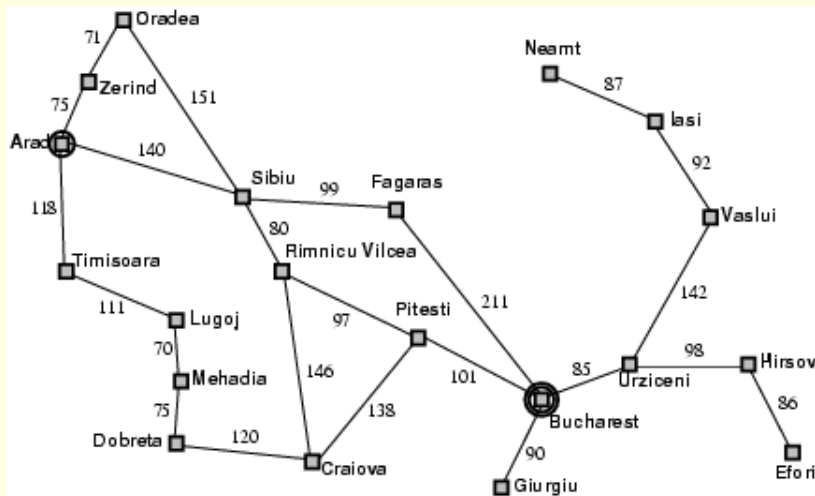
Fața **noduri** Sfarsit

Arad

Parcurgerea: Arad,

Adancime: 0

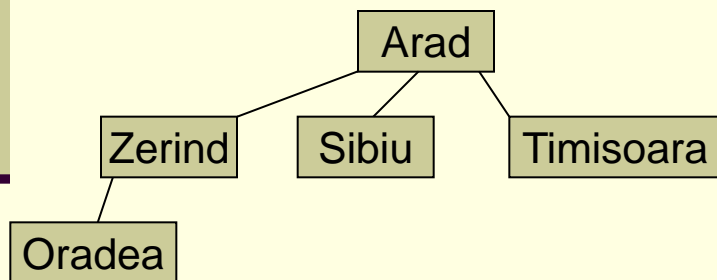
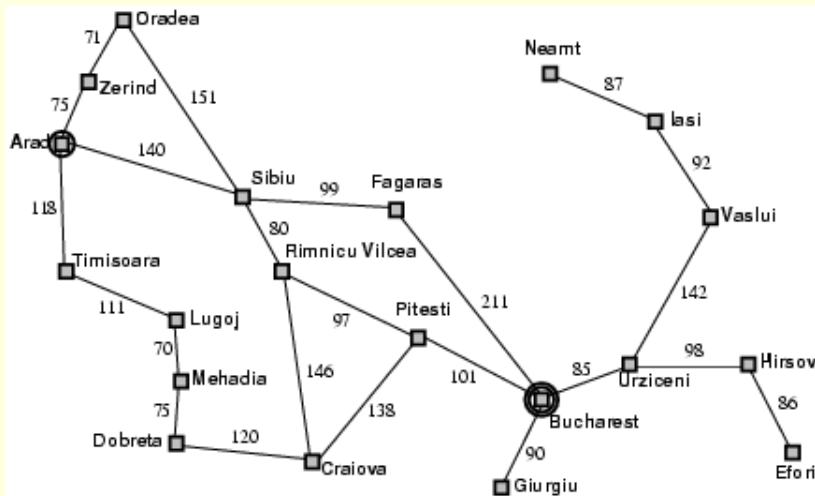
Cautarea limitata in adancime



Parcurgerea: Arad,

Adancime: 1

Cautarea limitata in adancime

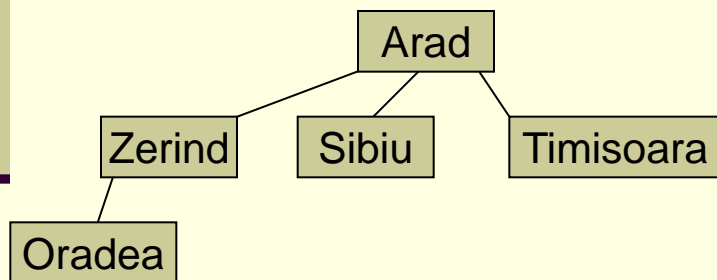
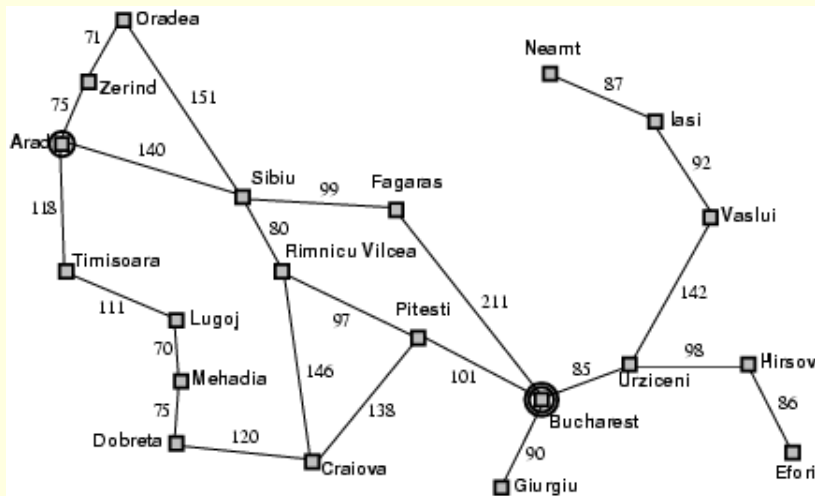


Fața	noduri	Sfarsit	
Zerind	Sibiu	Timisoara	

Parcurgerea: Arad, Zerind,

Adancime: 1

Cautarea limitata in adancime

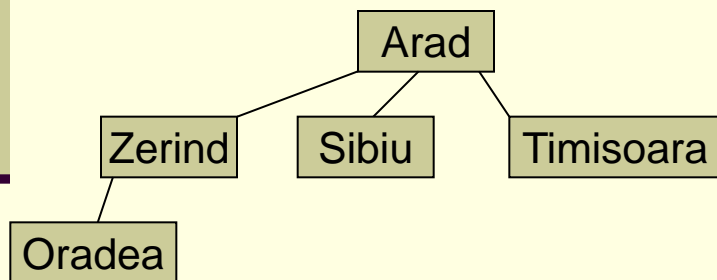
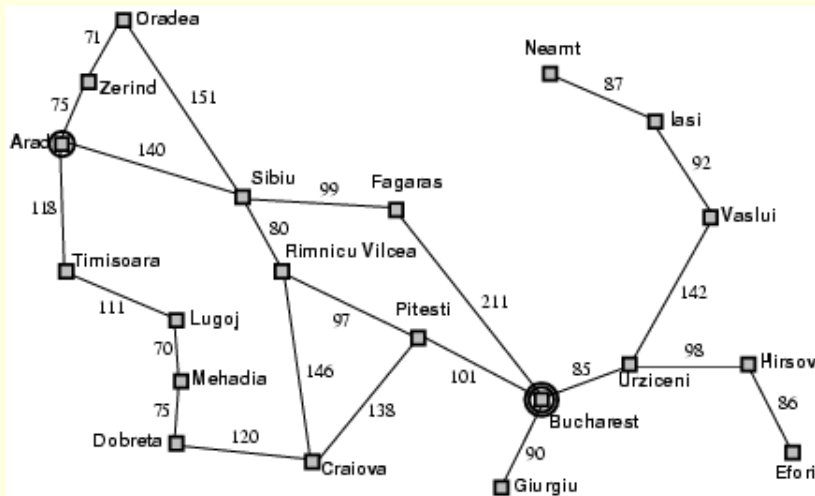


Fața	noduri	Sfarsit
Oradea	Sibiu	Timisoara

Parcurgerea: Arad, Zerind, Oradea

Adancime: 2

Cautarea limitata in adancime

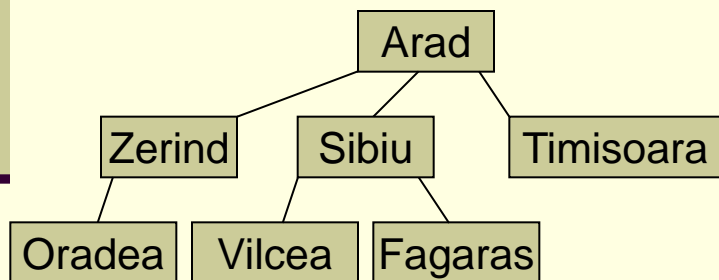
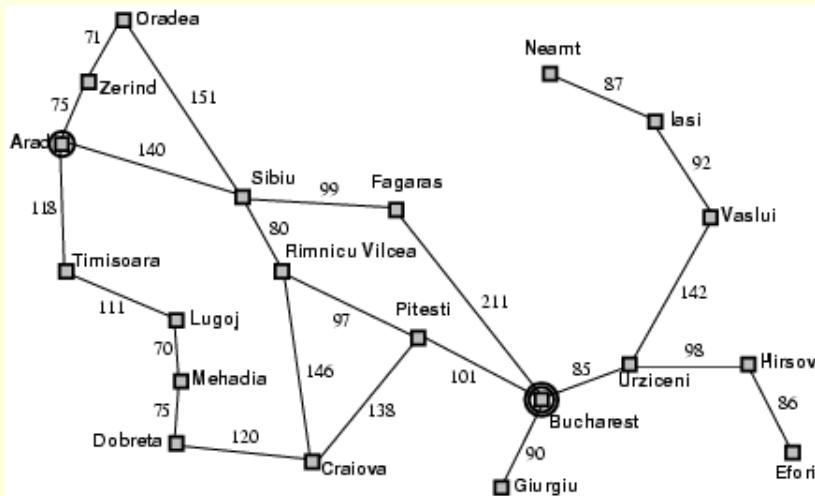


Fața	noduri	Sfarsit
Sibiu	Timisoara	

Parcurgerea: Arad, Zerind, Oradea, Sibiu

Adancime: 1

Cautarea limitata in adancime

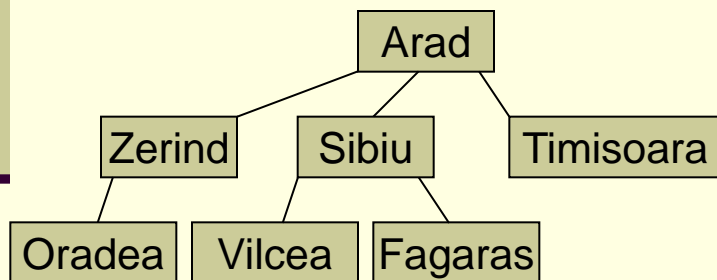
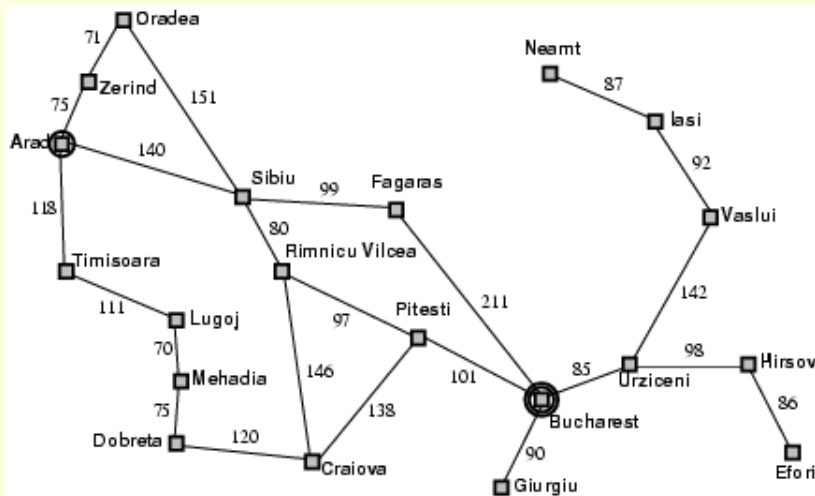


Fața	noduri	Sfarsit
Sibiu	Timisoara	

Parcurgerea: Arad, Zerind, Oradea, Sibiu

Adancime: 1

Cautarea limitata in adancime

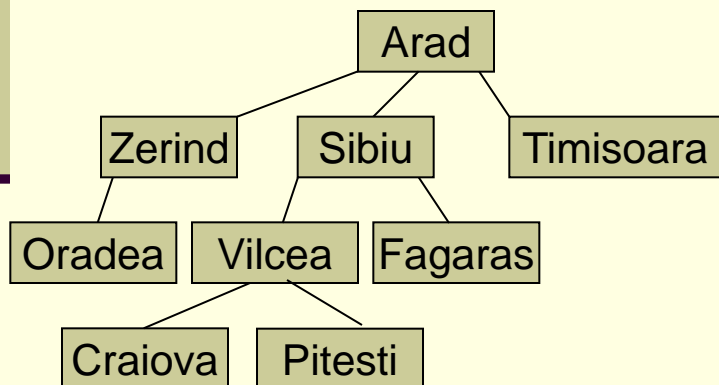
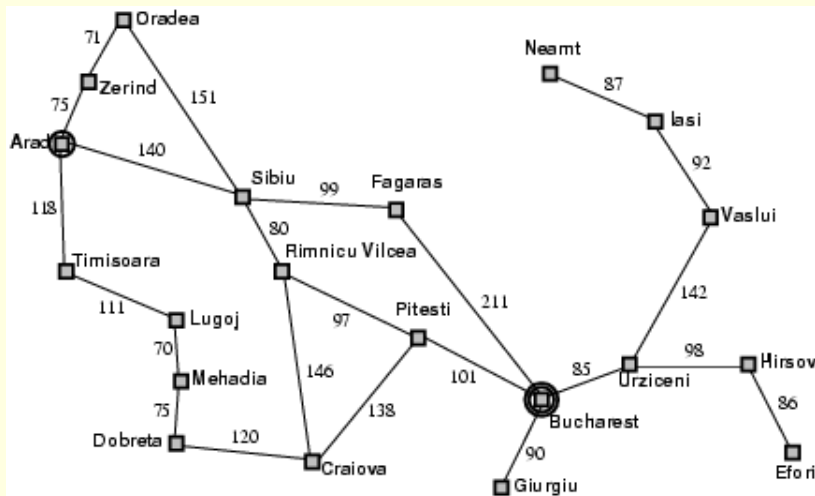


Fața	noduri	Sfarsit
Vilcea	Fagaras	Timisoara

Parcurgerea: Arad, Zerind, Oradea, Sibiu, Vilcea

Adancime: 2

Cautarea limitata in adancime

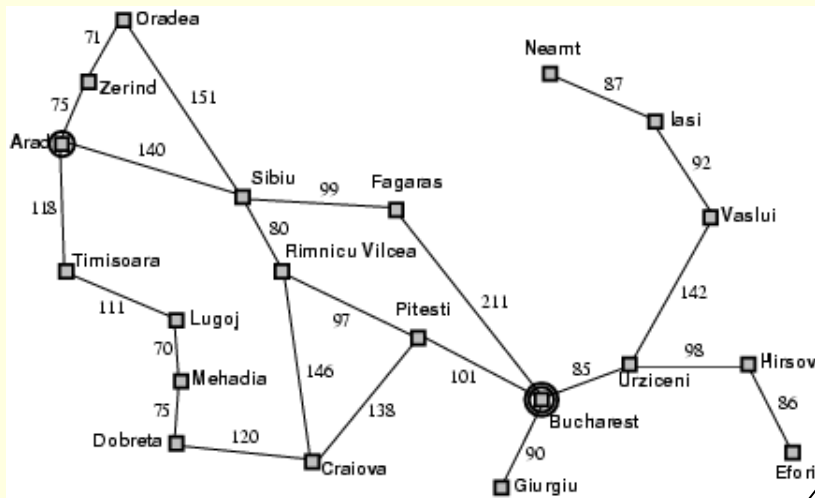


Fața	noduri	Sfarsit
Vilcea	Fagaras	Timisoara

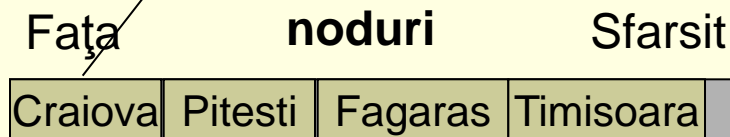
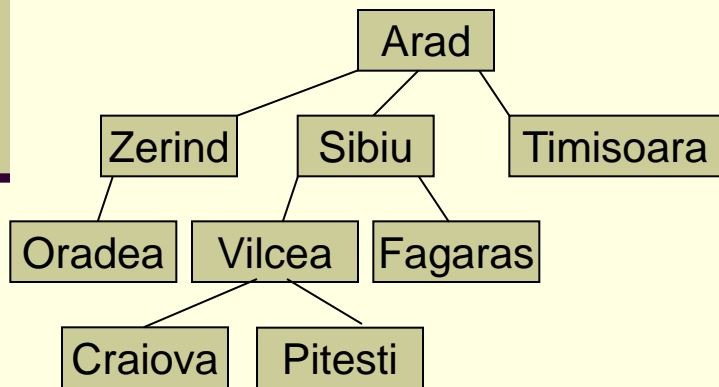
Parcurgerea: Arad, Zerind, Oradea, Sibiu, Vilcea

Adancime: 3

Cautarea limitata in adancime



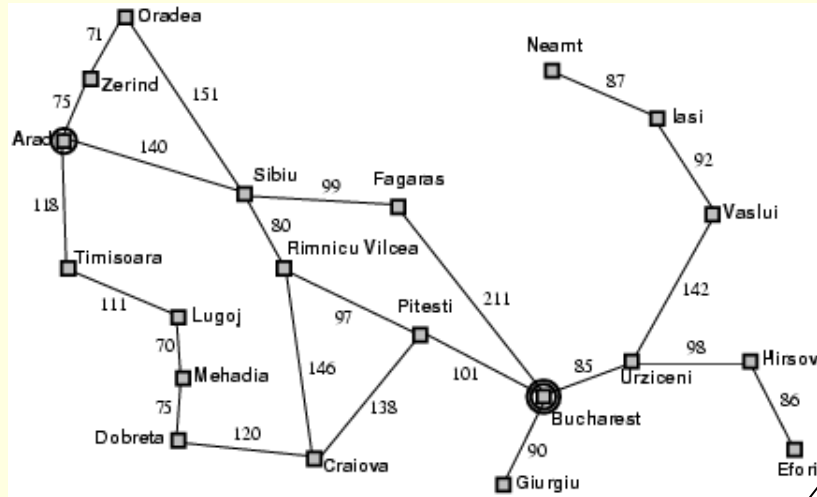
Nu este nodul tinta!!



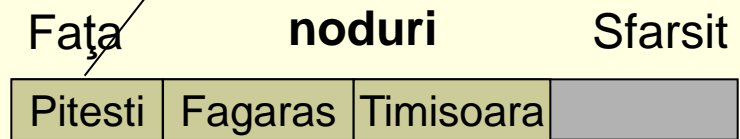
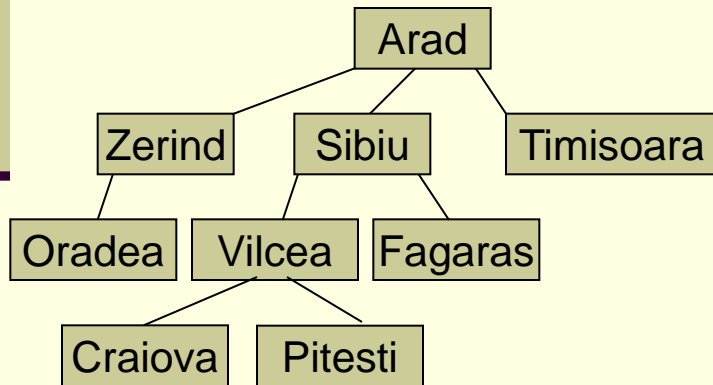
Parcurgerea: Arad, Zerind, Oradea, Sibiu, Vilcea, Craiova

Adancime: 3

Cautarea limitata in adancime



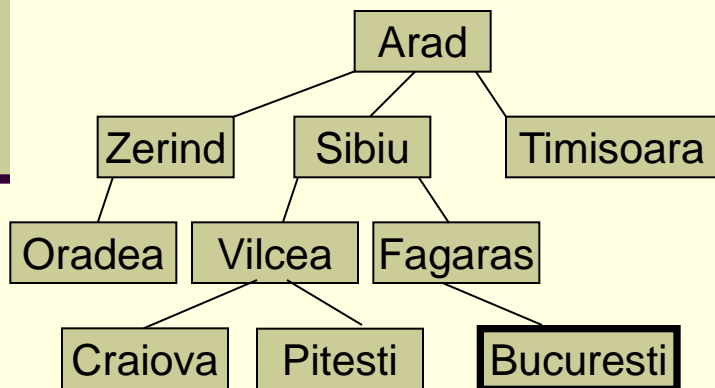
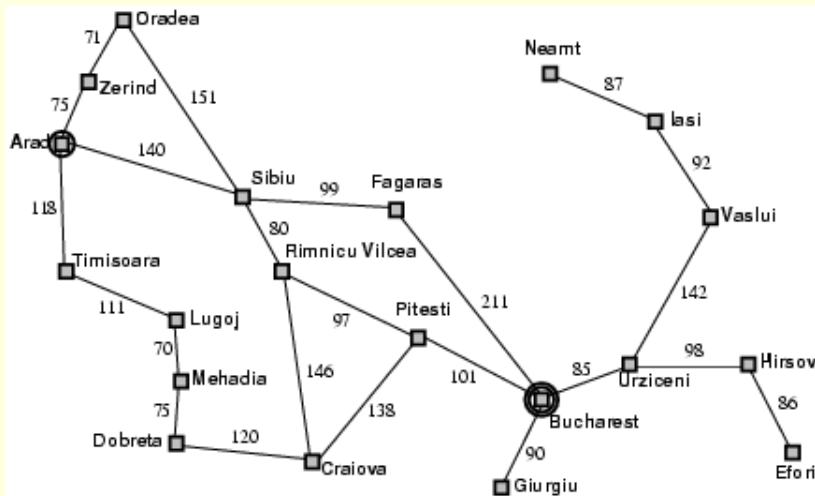
Nu este nodul tinta!!



Parcurgerea: Arad, Zerind, Oradea, Sibiu, Vilcea, Craiova, Pitesti

Adancime: 3

Cautarea limitata in adancime

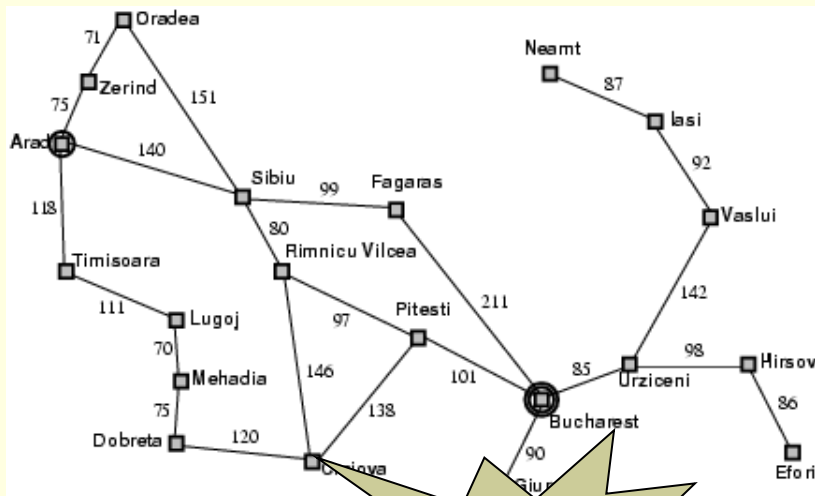


Fața	noduri	Sfarsit
Fagaras	Timisoara	

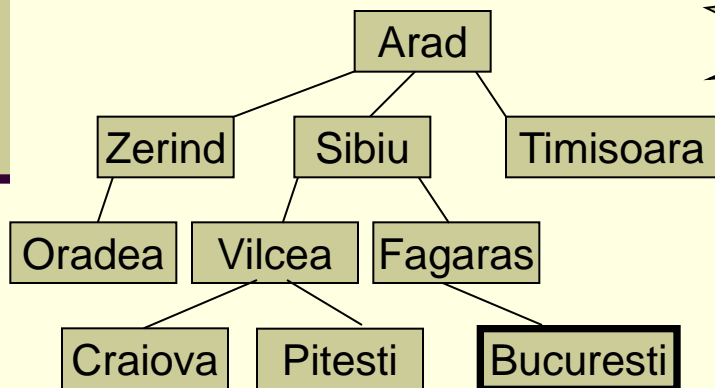
Parcurgerea: Arad, Zerind, Oradea, Sibiu, Vilcea, Craiova, Pitesti, Fagaras

Adancime: 2

Cautarea limitata in adancime



Nod tinta!



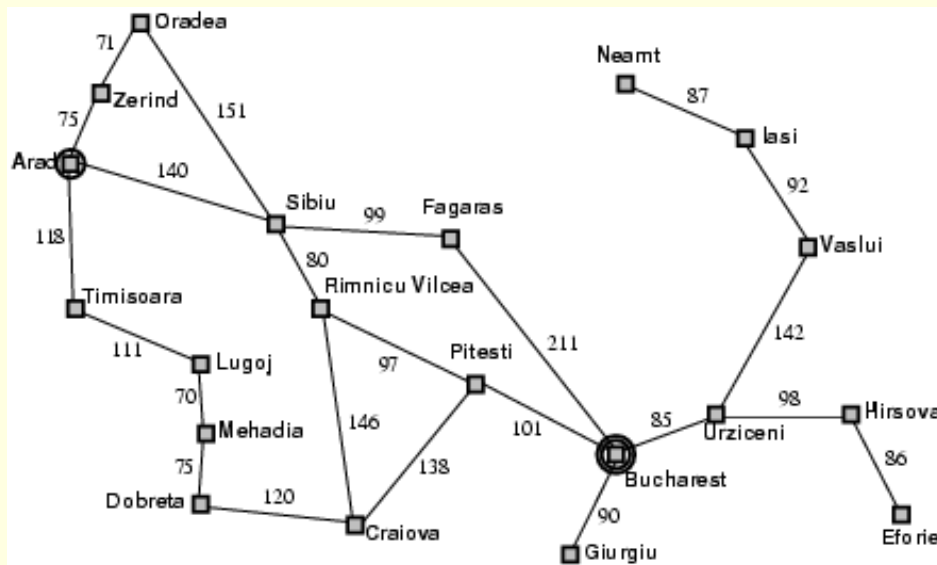
Fața **noduri** Sfarsit

Bucuresti | Timisoara |

Parcurgerea: Arad, Zerind, Oradea, Sibiu, Vilcea, Craiova, Pitesti, Fagaras, Bucuresti.

Adancime: 3

Exercitiu



Fața

noduri

Sfarsit

Gasiti o ruta de la Bucuresti la Rimnicu Vilcea folosind parcurgerea limitata in adancime cu limita 3.

Desenati arborele, scrieti parcurgerea si continutul pentru noduri la fiecare pas.

Parcurgerea: Bucuresti, ..., Rm. Vilcea

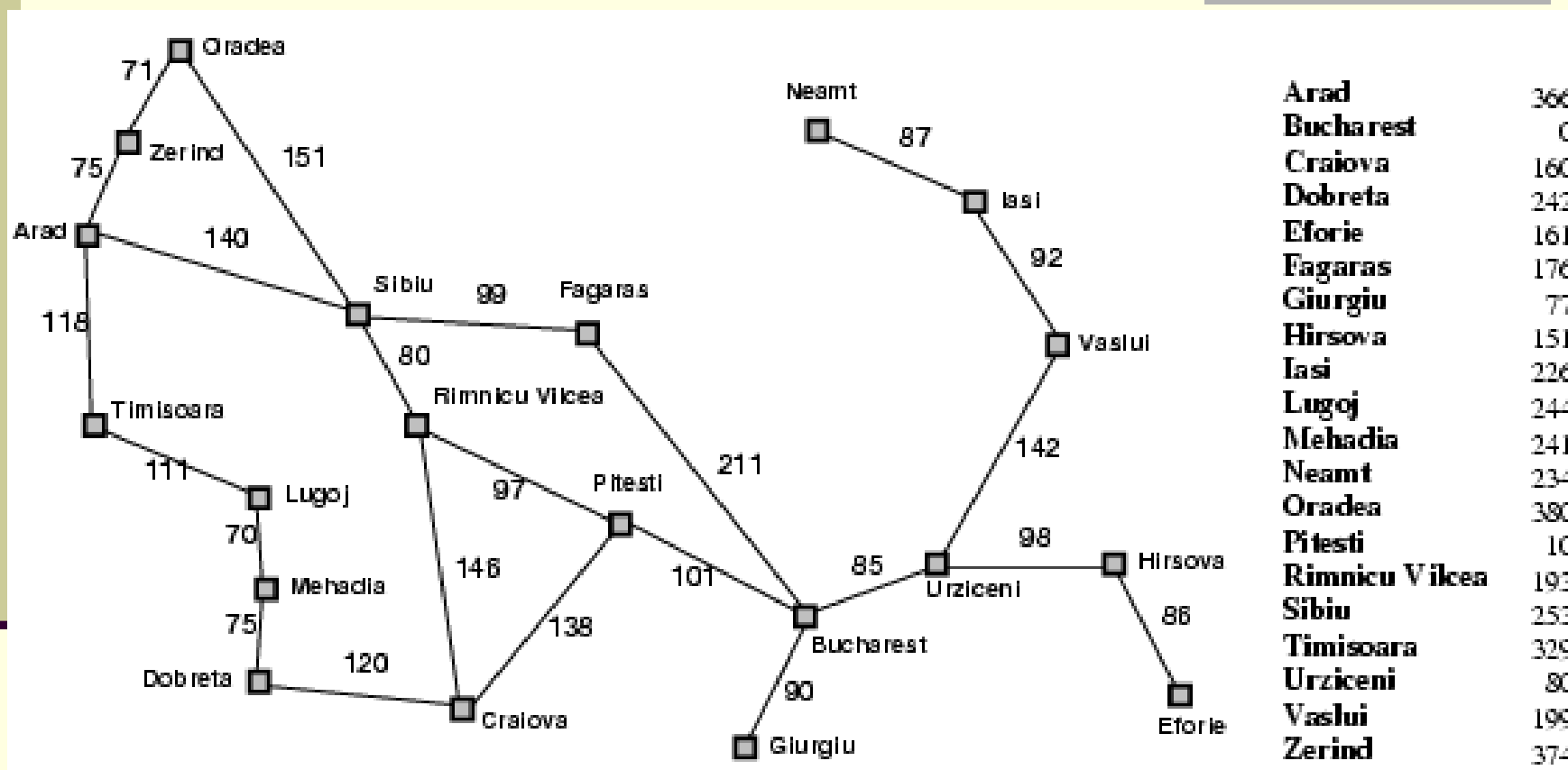
Cautarea Greedy

- Se bazeaza pe faptul ca trebuie minimizat costul de ajungere la nodul tinta.
- Concluzie: nodul care reprezinta starea care este cea mai aproape de starea tinta este intotdeauna expandat primul.
- La cele mai multe probleme, costul de a ajunge de la o stare la starea finala nu poate determinat exact, doar estimat.
- O functie care estimeaza astfel de costuri se numeste **functie euristica** si este notata de obicei cu h .

Cautarea Greedy

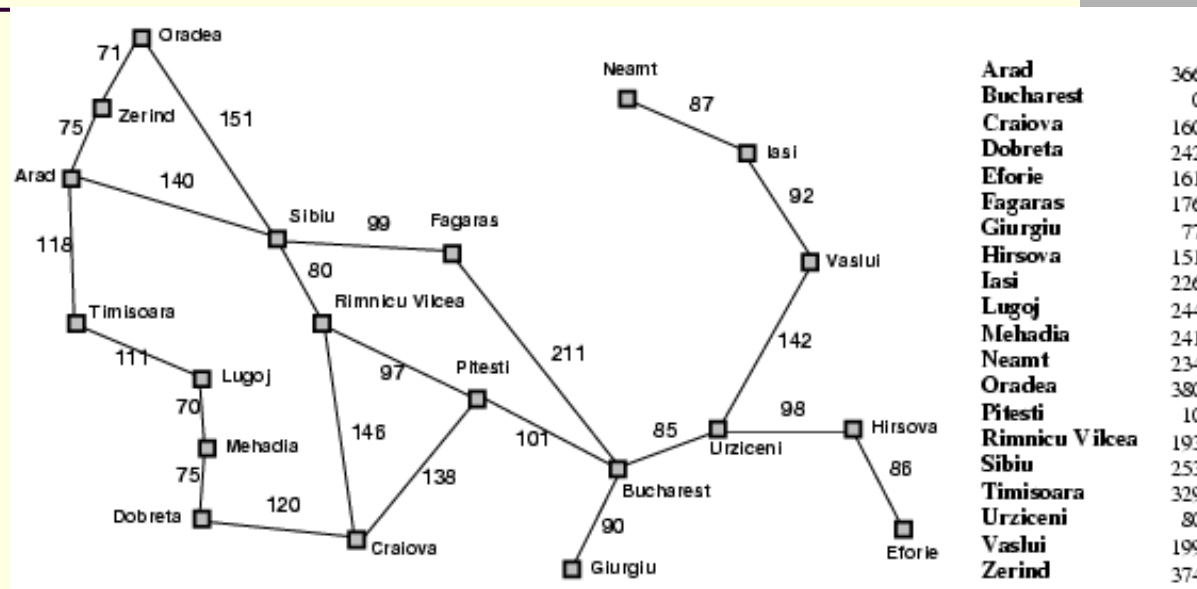
- $h(n)$ = costul estimat pentru cel mai scurt drum de la nodul n pana la starea tinta.
 - Daca n este chiar nodul tinta, atunci $h(n) = 0$.
- O cautare *intai cel mai bun* care utilizeaza asemenea functie euristica se numeste **cautare greedy**.

Avem distanțele până la București



- $h(n)$ = distanța în linie dreaptă de la orașul n până la București.

Greedy

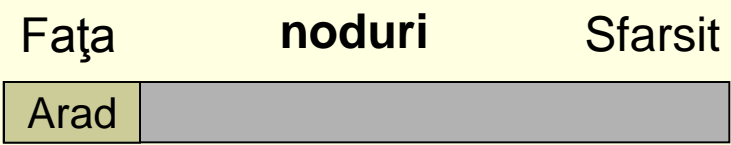
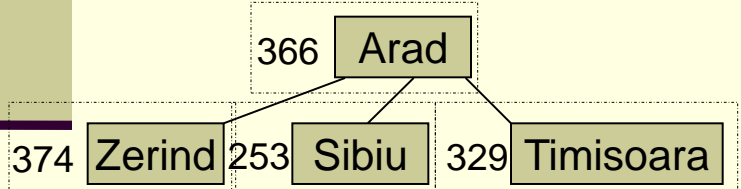
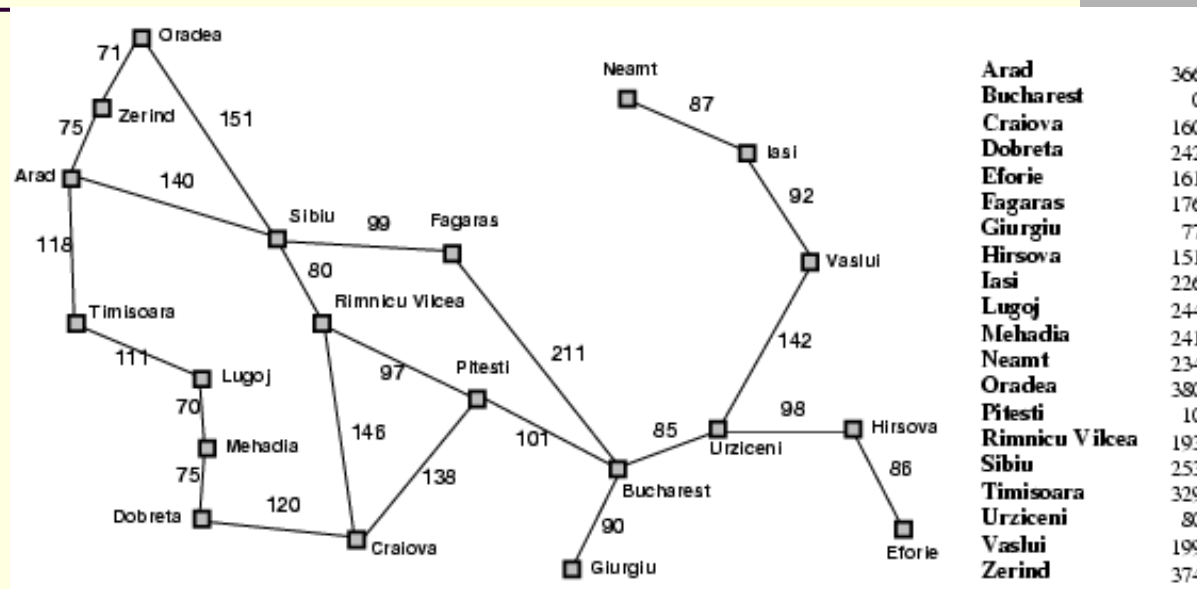


366 Arad

Fața	noduri	Sfarsit
Arad		

Parcursirea: Arad,

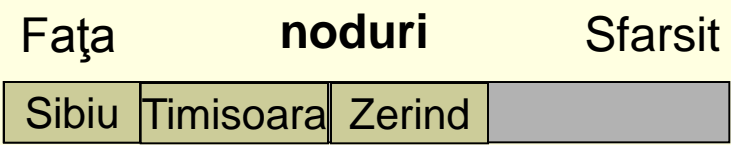
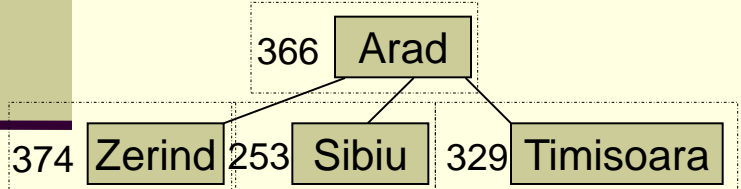
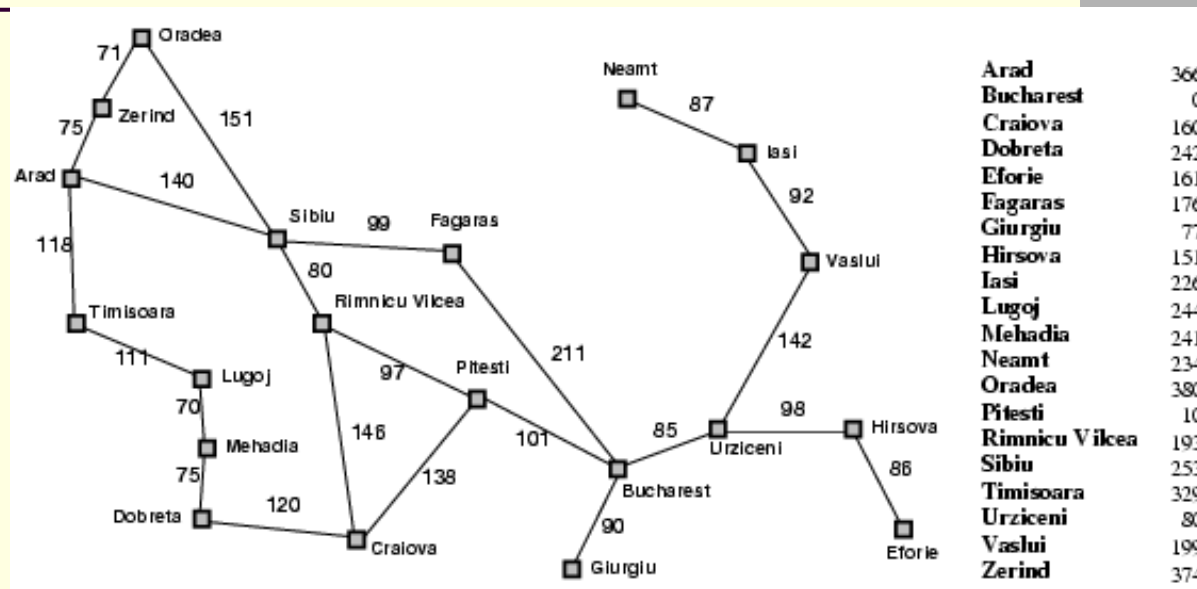
Greedy



Se adauga in noduri, din fața, incepand cu nodul cu evaluarea cea mai buna (orasul aflat la cei mai putini km, in acest caz).

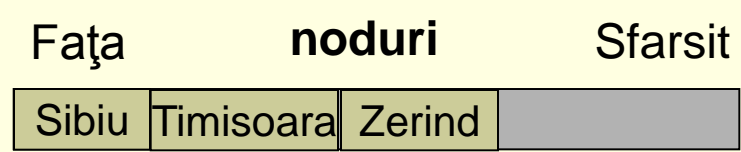
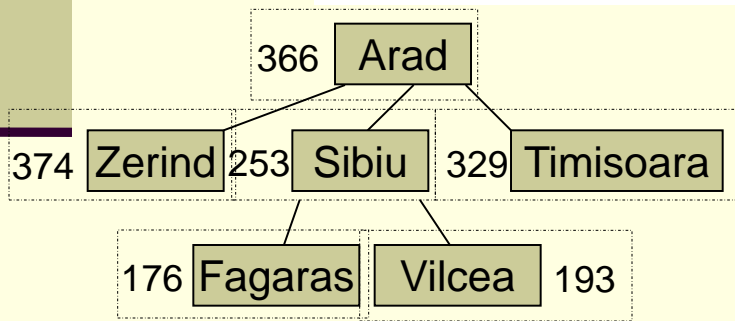
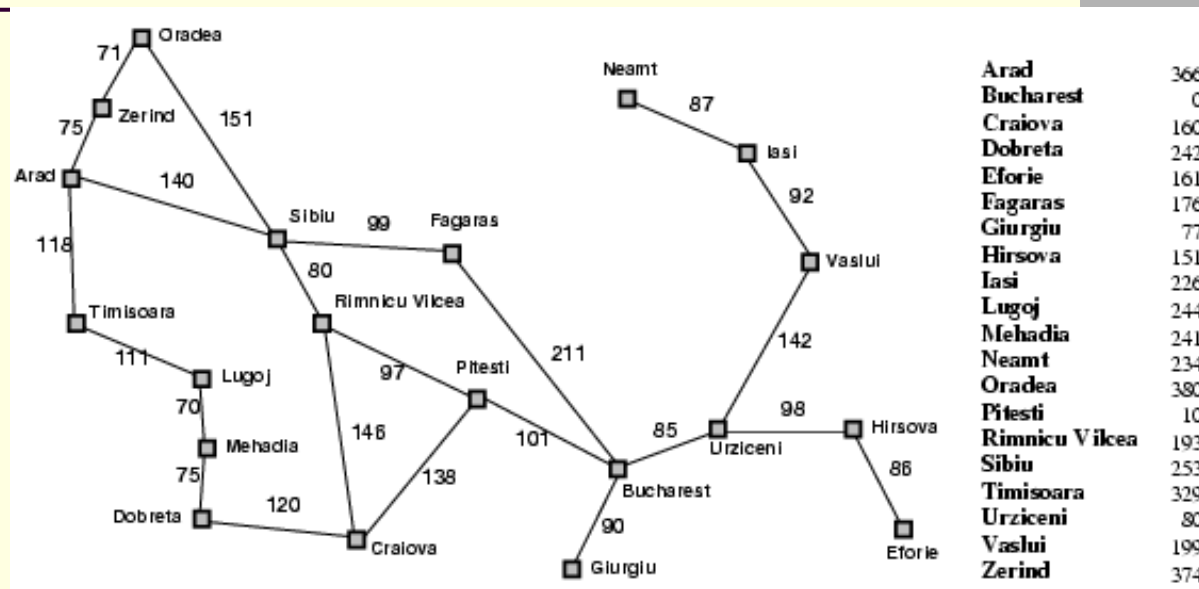
Parcurserea: Arad,

Greedy



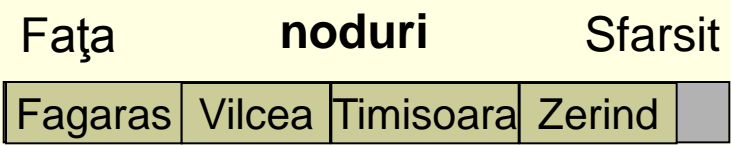
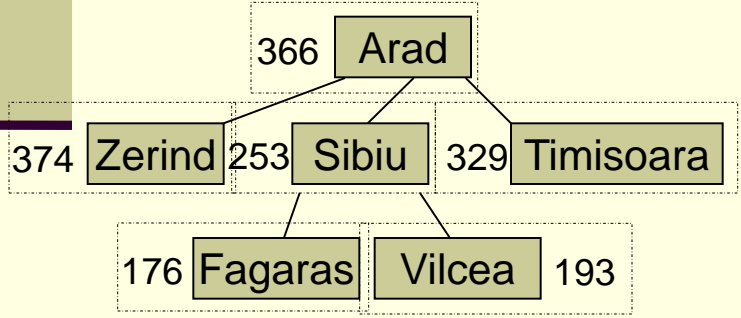
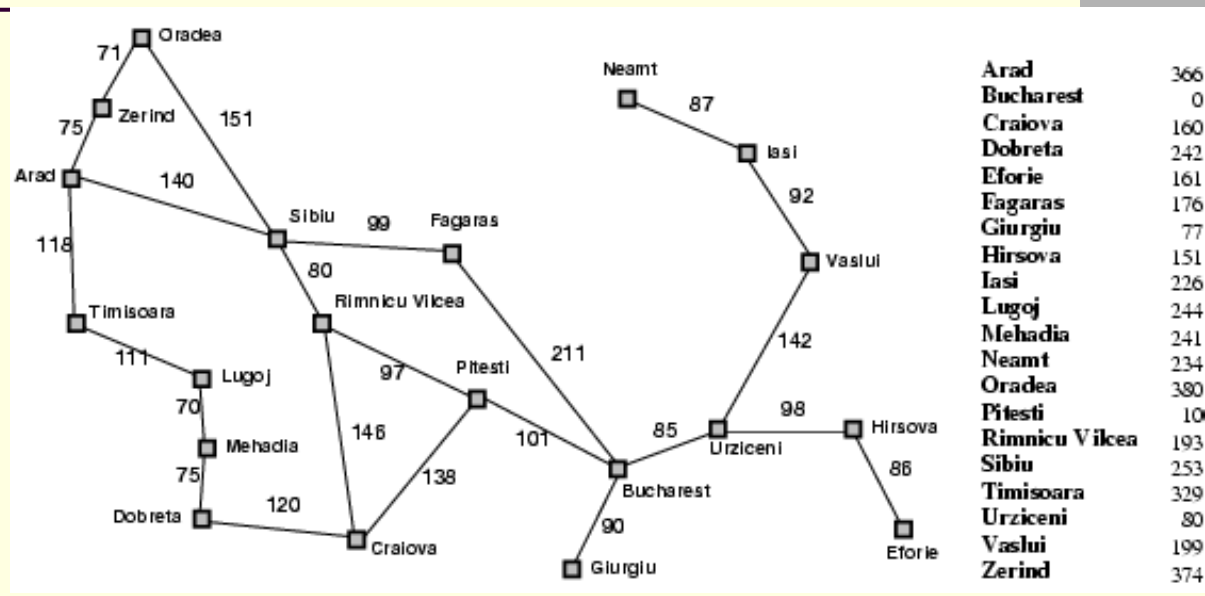
Parcurgerea: Arad,

Greedy



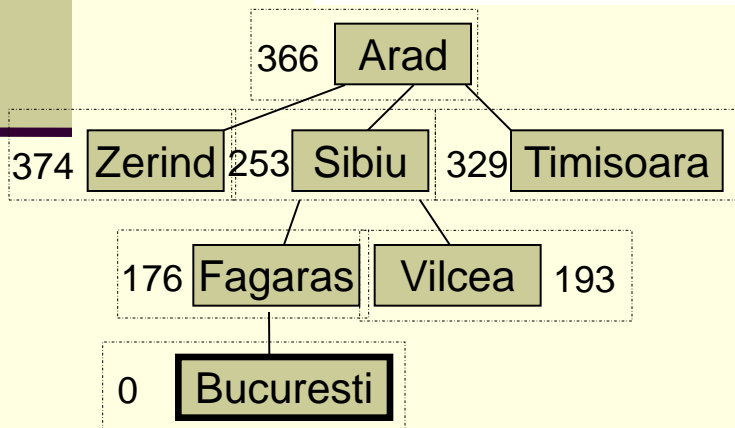
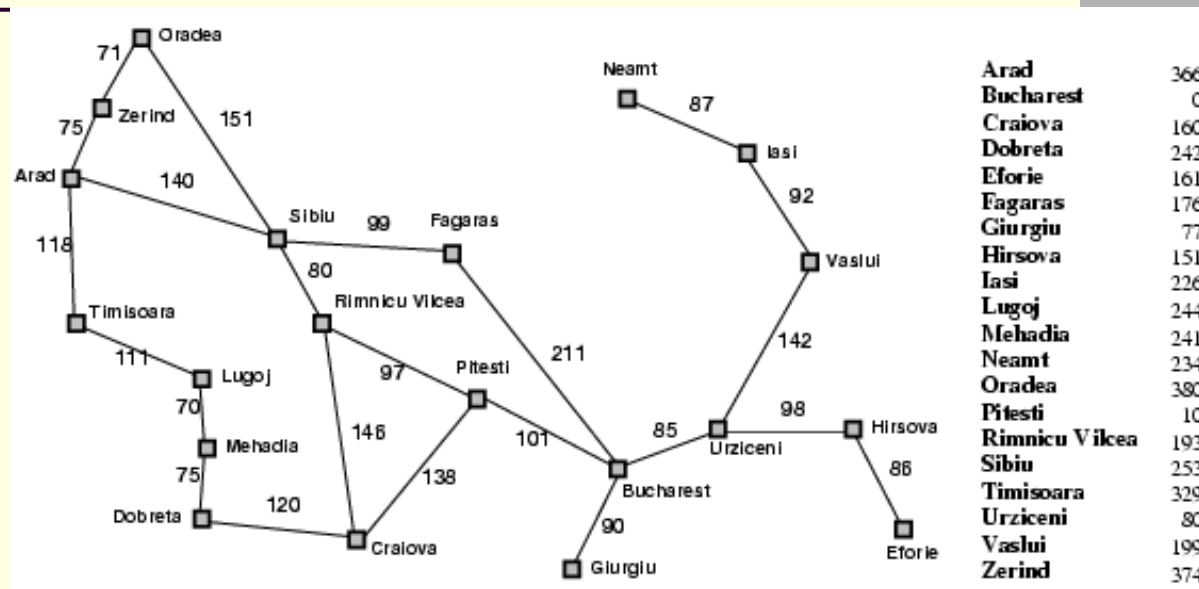
Parcursarea: Arad, Sibiu

Greedy



Parcursarea: Arad, Sibiu

Greedy

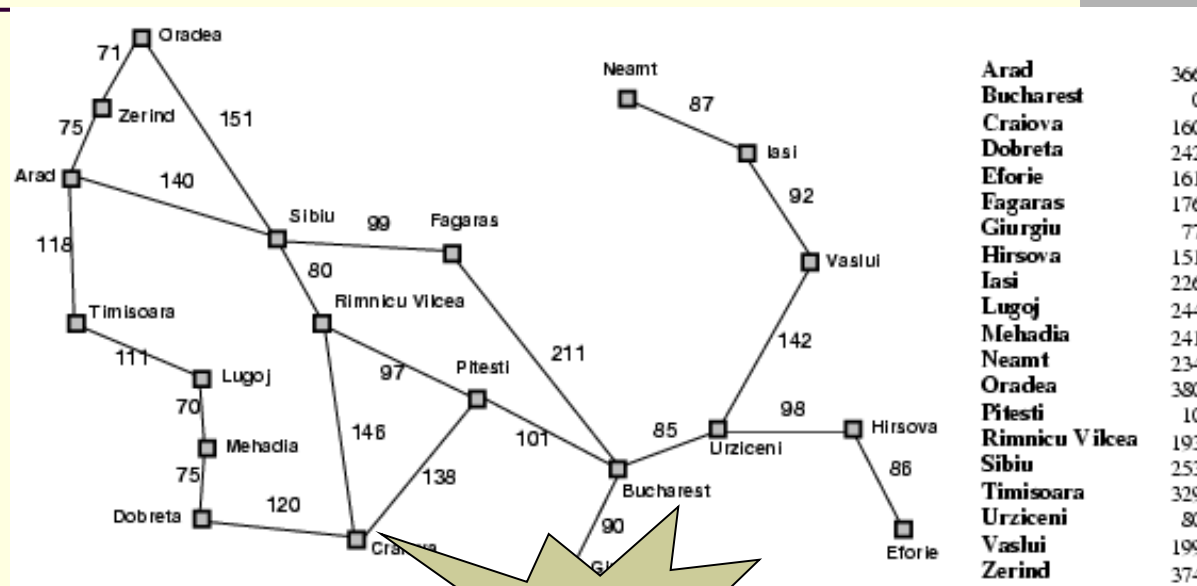


Fața noduri Sfarsit

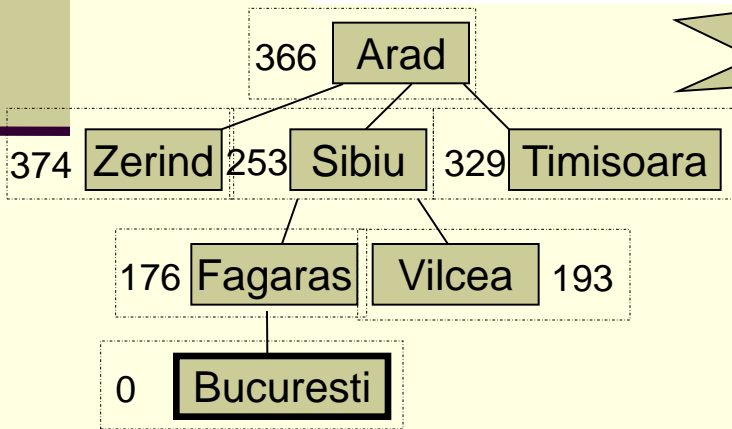
Fagaras	Vilcea	Timisoara	Zerind	
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Parcuregere: Arad, Sibiu, Fagaras

Greedy



Nod tinta!



Fața noduri Sfarsit

Bucuresti | Vilcea | Timisoara | Zerind |

Parcuregere: Arad, Sibiu, Fagaras, Bucuresti.

Tema

**Doua
puncte la
examenul
final!**

- Folosind cautarea Greedy, rezolvati puzzle-ul cu 8 valori folosind pe rand euristicile h_1 si h_2 .
- h_1 = numarul de cifre care sunt gresit pozitionate.

	2	3
1	4	6
8	7	5

 $= 5$
- h_2 = suma mutarilor necesare pentru ca toate cifrele sa ajunga la starea tinta ca si cum toate celelalte casute ar fi goale.

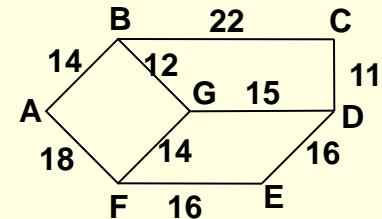
	2	3
1	4	6
8	7	5

 $= 0 + 0 + 1$
 $+ 1 + 0 + 1$
 $+ 1 + 2 = 6$
- Deplasarile se pot face numai pe orizontala si verticala.

Exercitiu - Cautarea informata

- Consideram asezarea a sapte orase ca in figura de mai jos. Scopul este ca, pornind din starea initiala D, sa ajungem in starea finala A. Distantele din figura sunt cele rutiere care se gasesc intre orase (deci nu in linie dreapta). Distantele in linie dreapta de la fiecare oras catre orasul A sunt urmatoarele:

- D: 30 G: 14
- C: 24 B: 11
- E: 21 F: 9



- Se cere
- Sa se calculeze distanta de la D la A folosind cautarea Greedy. Justificati.
- Acelasi lucru folosind cautarea A*.

Exercitiu

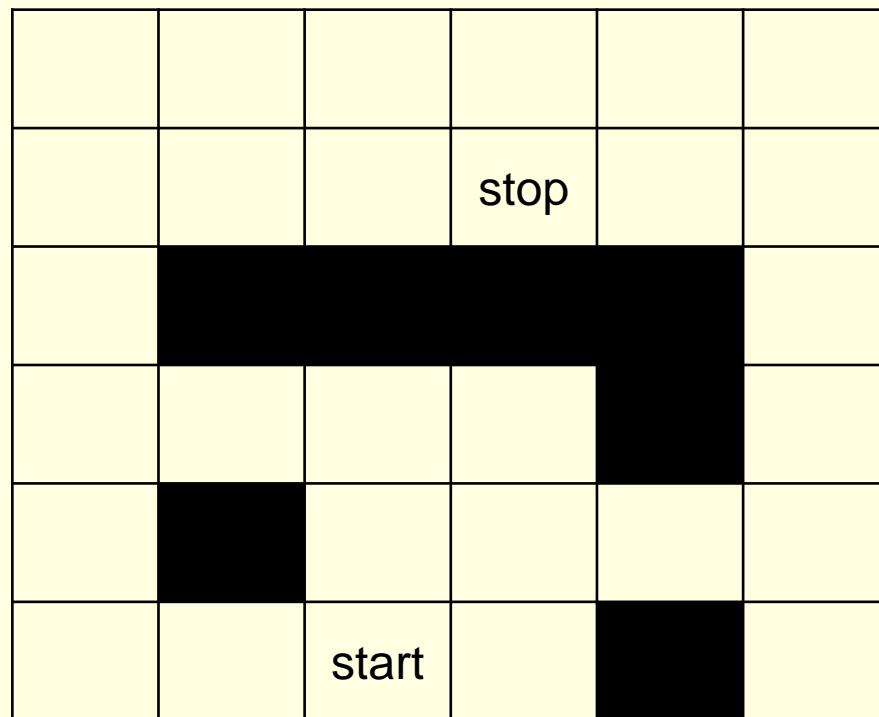
- Consideram distantele directe dintre 9 puncte date ca in tabelul de mai jos. Cazul in care intr-o casuta din tabel nu este trecuta nicio valoare semnifica faptul ca nu exista un drum direct intre cele doua puncte (de exemplu, intre A si C). Sa se aplice cautarea bidirectionala pentru gasirea drumului de la J la A, astfel incat din J sa se porneasca cu cautarea cu cost uniform, iar din A cu cautarea in latime: reprezentati arborii si scrieti ruta obtinuta in final.

	A	B	C	D	E	F	G	H	J
A	0	10	-	-	7	-	-	-	-
B	10	0	2	-	-	5	-	-	-
C	-	2	0	10	-	4	11	-	-
D	-	-	10	0	12	7	-	-	-
E	7	-	-	12	0	4	-	-	-
F	-	5	4	7	4	0	-	8	-
G	-	-	11	-	-	-	0	-	10
H	-	-	-	-	-	8	-	0	15
J	-	-	-	-	-	-	10	15	0

Exercitiu

- Considerăm problema găsirii unei rute în figura de mai jos de la start la stop.
- Agentul se mută un pătrat la fiecare pas vertical sau orizontal.
- Nu se poate deplasa în pătratele hasurate.
- 1. Etichetați cu litere în ordine alfabetică pătratele dacă se utilizează o căutare Greedy.

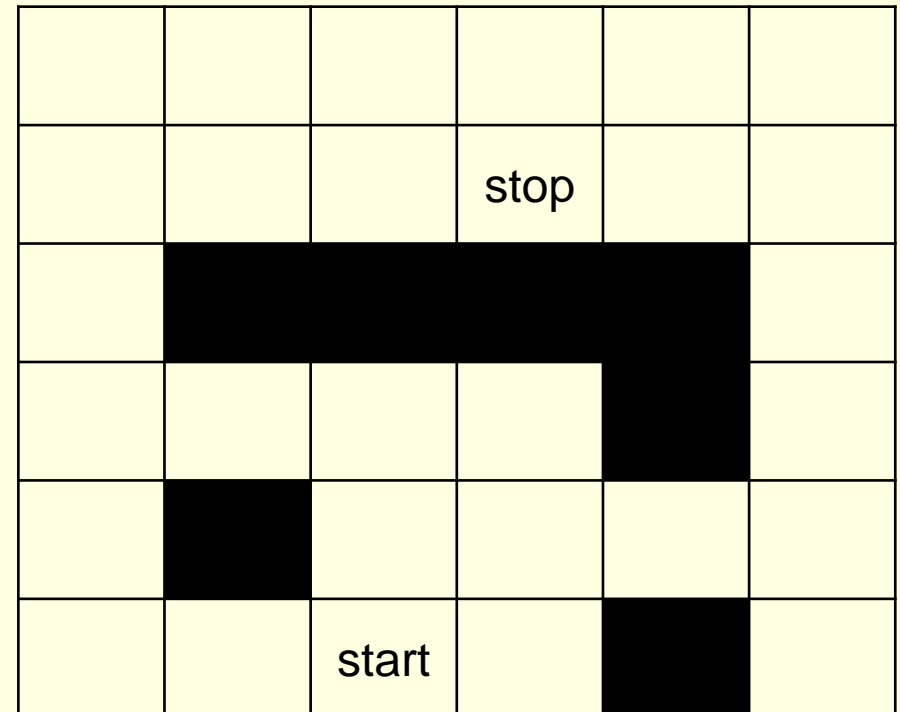
Pentru aproximare, folosiți distanța Manhattan – numărul de pătrate vizitate în direcția x + pătratele în direcția y până la tinta.



Nu se ține cont de pătratele hasurate pentru distanța Manhattan

Exercitiu

- Consideram problema gasirii unui rute in figura de mai jos de la start la stop.
- Agentul se muta un patrat la fiecare pas vertical sau orizontal.
- Nu se poate deplasa in patratele hasurate.
- 2. Etichetati cu litere in ordine alfabetica patratele daca se utilizeaza o cautare A^* .
- Pentru aproximare, folositi distanta Manhattan.



Exercitiu

- Considerăm problema găsirii unei rute în figura de mai jos de la start la stop.
- Agentul se mută un pătrat la fiecare pas vertical sau orizontal.
- Nu se poate deplasa în pătratele hasurate.
- 3. Presupunem că graful se extinde la infinit în toate direcțiile. start și stop rămân la aceleși locații, la fel și pătratele negre. Ce metodă nu mai găsește nicio soluție?

